

# CO<sub>2</sub> transport: Data and models – a review

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## Abstract

This review considers data and models for CO<sub>2</sub> transport. The thermophysical properties of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures are needed as a basis for various models within CO<sub>2</sub> capture and storage (CCS). In particular, this is true for transient models of pipes and vessels. Here, the data situation for phase equilibria, density, speed of sound, viscosity and thermal conductivity is reviewed, and property models are considered. Further, transient flow data and models for pipes are reviewed, including considerations regarding running-ductile fractures, which are essential to understand for safety. A depressurization case study based on recently published expansion-tube data is included as well. Non-equilibrium modelling of flow and phase equilibria are reviewed. Further, aspects related to the transport of CO<sub>2</sub> by ship are considered. Many things are known about CO<sub>2</sub> transport, e.g., that it is feasible and safe. However, if full-scale CCS were to be deployed today, conservative design and operational decisions would have to be made due to the lack of quantitative validated models.

*Keywords:* CO<sub>2</sub> transport, fluid dynamics, thermodynamics, thermophysical properties, depressurization, decompression,

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## 1. Introduction

In the two-degree scenario (2DS) of the International Energy Agency [1], which is one possible way of reaching the two-degree goal, CO<sub>2</sub> capture and storage (CCS) contributes to reducing the global CO<sub>2</sub> emissions by about six billion tonnes per year in 2050. To achieve this scenario, CO<sub>2</sub> must be transported from the points of capture to the storage sites. A large fraction of the captured CO<sub>2</sub> is likely to be transported in pipeline networks. Pipeline transport of CO<sub>2</sub> is different from that of natural gas in a number of ways. First, the CO<sub>2</sub> will normally be in a liquid or dense liquid state [2, 3], whereas the natural gas most often is in a dense gaseous state, see e.g. Aursand *et al.* [4]. Second, depending on the capture technology, the CO<sub>2</sub> will contain various impurities [5–7], which may, even in small quantities, significantly affect the thermophysical properties [8, 9]. The thermophysical properties, in their turn, influence the depressurization and flow behaviour [10]. Transport of CO<sub>2</sub> by pipeline is in operation for the purpose of enhanced oil recovery (EOR), mainly in the USA [11, 12]. The CCS case is likely to be different, due to different impurities, and the proximity to densely populated areas. Thus, there is a need to develop modelling tools which can aid in the safe and economical design and operation of CO<sub>2</sub>-transport pipelines.

Flow models for CO<sub>2</sub> transport should be able to take a number of phenomena into account. As already alluded to, multiple

chemical components need to be catered for. Already in a single-phase case, CO<sub>2</sub> mixtures from different capture technologies will give different dynamic behaviour in pipeline transport [13]. Depending on the conditions, hydrates [14], or other solids, may form. Two-phase liquid-vapour flow may also occur, even if the pipeline is designed to be operated in the single-phase region. This may be due to varying CO<sub>2</sub> supply [15], or during transient events, such as start-up, shut-in or depressurization [16–18]. During these events, among other things, it is important to be able to estimate the temperatures, since the construction materials may have a minimum temperature below which they begin to lose their toughness, e.g. the ductile-brittle transition temperature of steel. Furthermore, it is of great importance to be able to calculate the single-phase and two-phase (mixture) speed of sound. This is because a given pipeline filled with CO<sub>2</sub> is more susceptible to running-ductile fracture than if filled with natural gas [2, 19, 20], and the running fracture is governed by a ‘race’ between the fracture velocity and the speed of sound.

The dispersion of CO<sub>2</sub> resulting from a leakage [21–24] is an input to risk assessments. To obtain realistic input boundary conditions to dispersion models, it is necessary to have good depressurization models for pipes and vessels.

Koornneef *et al.* [25] pointed out various knowledge gaps which affect the uncertainties of quantitative risk assessments for CO<sub>2</sub> pipelines. However, the fact that CO<sub>2</sub> pipelines have different challenges when compared to natural gas pipelines does not mean that CO<sub>2</sub>-pipeline networks will be associated with high risks. The study by Duncan and Wang [26] suggested a very small likelihood of having potentially lethal releases for CO<sub>2</sub> from pipelines, assuming, among other things, that fracture propensity can be successfully mitigated.

Due to the large investments associated with offshore pipelines,

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transportation by ship may be a viable alternative due to its flexibility, especially in a start-up phase with relatively low CO<sub>2</sub> volumes. Among the issues needing further attention, is the design of the offloading system, which also has to be compatible with the restrictions imposed by the storage site. Such considerations require modelling tools accurately representing the thermophysical properties of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures, including the vapour-liquid phase boundary and the precipitation of solids. Further, the emptying or depressurization of vessels have similarities with the depressurization of pipelines.

Regarding the content of other substances ('impurities') in the CO<sub>2</sub> to be transported, there appears to be at least two views. The first is that one should arrive at a 'transport specification' listing the maximum allowable content of impurities. The second is to perform knowledge-based optimization for each case. We believe that the latter approach may lead to a more efficient CCS system, preventing e.g. the oversizing of capture and conditioning plants. In the case of ship transport in particular, the liquefaction process should be optimized together with the capture process.

In view of the above, we want to review the state of the art with respect to data and models for transient two- and multiphase flow of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures in CO<sub>2</sub>-transport systems. Emphasis is put on developments having taken place after the reviews by Aursand *et al.* [4], Li *et al.* [8, 9], Gernert and Span [27], or on relevant subjects not covered therein. We put our boundary conditions around the transport system itself, focusing on thermo- and fluid dynamics in, and out of, pipes and vessels.

Although it would lead too far to enter into details in this paper, it should not be forgotten that the accuracy of a simulation not only depends on the accuracy of the physical model, but also on the employed numerical method. Numerical methods for multiphase flow models is a subject where there are still challenges with respect to robustness, accuracy and efficiency. For instance, numerical diffusion can smear out the resolution of a depressurization wave in a pipeline [28, 29]. The numerical methods employed to solve for the thermophysical properties also need to be highly consistent, robust and efficient. This is particularly true in conjunction with CFD methods, where the thermophysical properties are needed in each computational cell at each time step.

The remainder of this article is organized as follows. In Section 2 we review the data situation for phase equilibria, density, speed of sound, viscosity and thermal conductivity of CCS-relevant CO<sub>2</sub>-rich mixtures. Section 3 deals with property models and briefly discusses implementation in fluid-dynamic models and flow through restrictions, which is relevant for decompression calculations. In Section 4, we review published data and models for transient multiphase flow of CO<sub>2</sub>-rich mixtures in pipes. In particular, we include pipe-depressurization case study. Section 5 considers ship transport of CO<sub>2</sub>. The study is concluded in Section 6.

## 2. Thermophysical property data

Knowledge of the relevant thermophysical properties of the relevant fluids is needed to optimize CO<sub>2</sub> transport with respect

to economy, operability and safety. A few examples will be provided in the following. We will then review the situation regarding thermophysical property data for CO<sub>2</sub>-rich CCS-relevant mixtures.

In pipeline transport it is usually desirable to have the fluids in dense phase, and hence knowledge of the vapour-liquid *phase behaviour* is essential [30, 31]. Accurate knowledge of vapour-liquid phase behaviour is particularly important when water is present in the CO<sub>2</sub>-rich fluid to be transported, since even small amounts of water may lead to accelerated corrosion, in particular when in combination with other impurities [32–36]. At even lower water concentrations, CO<sub>2</sub> may form hydrates [37], in particular in combination with methane [38]. Phase behaviour will also be an important factor to determine the temperature and pressure characteristics of the CO<sub>2</sub>-rich liquid in ship transport, and is particularly important in the design of the liquefaction process, for instance in order to avoid solid-state formation. Finally, phase behaviour models are very important to predict transient phenomena such as sudden (de-)pressurization of pipelines [39] and liquid loading and unloading of vessels.

For dimensioning of both pipelines and vessel size in ship transport, knowledge of the *density* as a function of pressure, temperature and composition is required. Density is also important for the design of important processing equipment such as compressors and pumps. In future large-scale CCS, accurate flow metering will be needed, both for government control and to facilitate a working CCS market and in order to optimize the processes involved. Many of the most relevant methods used today for fiscal natural gas metering are volumetric and hence need accurate density information for the transported mixtures.

*Speed of sound* has readily apparent importance in determining the flow rate in choked flow or in order to model any transient phenomena involving pressure waves. However, in addition, speed of sound often has an important role in the development and verification of equations of state (EOSs). The thermodynamic speed of sound is defined from the isentropic pressure variation with density, and for single-phase flow it is a purely thermodynamic function. In multiphase flow this is complicated by the interaction of the phases.

Among transport properties, *viscosity* is needed to estimate the pressure drop in pipes, reservoir modelling, as well as for the design of processing equipment. *Thermal conductivity* and *heat capacity* are needed for heat-transfer calculations, heat-exchanger design and a range of transient phenomena. Likewise, *diffusion coefficients* are needed to properly model e.g. reservoir behaviour and tank unloading.

Although the focus of this work is on CO<sub>2</sub> transport, thermophysical properties are also of high relevance in other sections of the CCS chain, both during capture, processing, injection and storage.

### 2.1. CCS capture product and transport fluid specifications

In real-life applications, the CO<sub>2</sub> to be transported will not be pure, but will be mixed with a certain amount of different impurities. As indicated in Table 1, the concentration range of different impurities in the CO<sub>2</sub> product from CCS capture

processes can be quite large, depending on the capture technology and e.g. the purity of the fuel. It should be clear that the high level of impurities from some of the capture processes will lead to thermophysical properties that are drastically different from that of pure CO<sub>2</sub>. For instance, the presence of only small amounts of dry air gases will increase the power consumption of transport chains [40], high levels of oxygen may be undesirable for instance in EOR and storage in depleted oil reservoirs, and toxic components may be unacceptable from regulator's point of view. The effects of water have already been discussed above. Hence, conditioning of the captured CO<sub>2</sub> product may be needed in many cases to enable efficient transport and storage. However, conditioning comes at a cost depending on the specified purity level, and hence, the levels of impurities allowed should be determined based on accurate models for the behaviour of the CO<sub>2</sub>-rich mixtures.

For the different CO<sub>2</sub> pipelines in operation today, there is no consensus with regard to the specifications of CO<sub>2</sub> product composition and operational pressure. For instance, the maximum water content specifications vary between 50 ppm and 630 ppm [41]. In the Sleipner project, Hansen *et al.* [42] even indicate that the water content is more than 1000 ppm, which could lead to hydrate formation or even water-rich liquid phase at prolonged shut-ins. From a corrosion perspective, this example has less general relevance due to the use of stainless steel, which will be too expensive in projects of larger scale. It should be noted that most of the US EOR pipelines are transporting gas from geological CO<sub>2</sub> sources, which, depending on the capture and conditioning process, have different compositions than what is expected in CCS systems. During the last decade, various CO<sub>2</sub> quality recommendations for CCS pipeline transport have been proposed [2, 5, 43–46]. They vary a lot, for instance when it comes to water content (50 to 500 ppm), other impurities and overall CO<sub>2</sub> purity (95 to 99.5 %).

## 2.2. Data situation for equilibrium properties

Relatively recently, a review by Gernert and Span [27] has mapped the availability of experimental data on various thermodynamic properties of mixtures containing CO<sub>2</sub>, H<sub>2</sub>O, N<sub>2</sub>, O<sub>2</sub>, Ar, and CO. The last experimental data points considered were from 2012. Li *et al.* [8] published a review on density and phase equilibria data on CO<sub>2</sub>-rich mixtures, with the last data considered being from 2002. Further, Li *et al.* [9] published a review on the data situation with regard to viscosity, thermal conductivity and diffusivity, with the last data points considered being from 2004. For fluid-phase equilibria, there is a series of articles covering high-pressure vapour-liquid equilibrium (VLE) measurements of many systems [47–53]. In order to get an up-to-date overview of data availability, free databases such as NIST's ThermoLit [54, 55] could be a useful source.

In the current work, a rather up-to-date overview of the data situation for phase behaviour, density, speed of sound, viscosity and thermal conductivity relevant for CCS will be provided. A warning is however warranted: Often data reviews are given in terms of parameters such as number of data points, pressure, temperature, and composition range. This information can in some cases be quite misleading. Firstly, there will often be large

regions without data between the bounds of the pressure, temperature and composition range. Secondly, the usefulness of the data will depend on their real accuracy. In practice, accuracy is often not indicated in the data source. If it is indicated, there could be large discrepancies between what is claimed and the reality. Hence, for modelling purposes, careful study and consistency checks of the actual data should be performed, where the data often are categorized as either primary data used for modelling or secondary data. In EOS-CG [27], the new mixing rules were based only on 14 % of the data points available for the respective binary systems. It is beyond the scope of this work to perform such a critical review, and hence even for the systems and properties with the most measurements, a satisfactory data situation cannot be claimed. However, the overview provided indicates the strong need for more measurement data for certain properties, conditions, and mixtures, and should provide a useful starting point for further data mining and analysis.

The results of the data survey are shown in Tables 2–8. The information provided for the systems covered includes the number of sources, the number of sources during the last 40 years, the location of references, the number of data points, and ranges in temperature, pressure, and composition. New data do not at all have to be better than historic data, but generally, both the measurement techniques and physical understanding of the different measurement principles have improved during the last decades. Secondary referencing using some existing reviews [8, 9, 27, 56–63] are used for some of the sources, both because some of these references go deeper into the data, and to limit the number of references in the current work somewhat. In the tables, the number of references provided by each secondary source is given in an exclusive manner, such that primary sources are only counted once.

For all properties, data have been surveyed for binary mixtures between CO<sub>2</sub> and the other components listed in Table 1, which we will call primary mixtures in the following. If no data are found for such a binary system for a given property, no entry is provided in the relevant table. For phase equilibrium, also data from binary mixtures with water as well as ternary mixtures are provided. The reason is that even a small presence of a second phase in CCS transport could have a large impact. For some of the properties, also pure CO<sub>2</sub> is considered because of the rather small number of experimental papers found.

### 2.2.1. Vapour-liquid-liquid equilibrium (VLE)

An overview of VLE data relevant for CCS is provided in Table 2. Regarding some important binary systems for CCS, like CO<sub>2</sub>-N<sub>2</sub>, CO<sub>2</sub>-CH<sub>4</sub>, and CO<sub>2</sub>-H<sub>2</sub>O, the reports of a number of recent experimental studies seem to indicate a satisfactory data situation. Nevertheless, gaps and inconsistencies have recently been pointed out. For instance, with regard to CO<sub>2</sub>-N<sub>2</sub>, it was argued in [65] that prior to recent measurements [65, 79], the data situation was not very satisfactory at high temperatures and around the critical pressure. This is illustrated around 298.15 K in Figure 1, where the presence of data is not equivalent to a satisfactory data situation. Recently, the data situation for CO<sub>2</sub>-O<sub>2</sub> has drastically been improved [82], and also the data situation for CO<sub>2</sub>-H<sub>2</sub> is now better than it used to be thanks to

Table 1: Lower ( $x_{i,\min}$ ) and upper ( $x_{i,\max}$ ) range of typical impurity mole fractions from different capture processes. From [9] based on data from [2].

	CO <sub>2</sub>	N <sub>2</sub>	O <sub>2</sub>	Ar	SO <sub>2</sub>	H <sub>2</sub> S/ COS	NO <sub>x</sub>	CO	H <sub>2</sub>	CH <sub>4</sub>	H <sub>2</sub> O	Amines	NH <sub>3</sub>
$x_{i,\min}$ (%)	75	0.02	0.04	0.005	<10 <sup>-3</sup>	0.01	<0.002	<10 <sup>-3</sup>	0.06	0.7	0.005	<10 <sup>-3</sup>	<10 <sup>-3</sup>
$x_{i,\max}$ (%)	99	10	5	3.5	1.5	1.5	0.3	0.2	4	4	6.5	0.01	3

Table 2: VLE data for CCS-relevant systems.

System (1)-(2)-(3)-(4)	# Sources		Location of References	# Points	Data ranges		
	Total	1975→			$T$ (K)	$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub> -N <sub>2</sub>	34	26	12 in [8] + 12 in [27] + [65, 72–80]	> 700	208–303	0.6–21.4	0.15–0.999
CO <sub>2</sub> -O <sub>2</sub>	8	2	5 in [8] + 1 in [27] + [81, 82]	> 292	218–298	0.9–14.7	0.15–0.99
CO <sub>2</sub> -Ar	4	2	2 in [8] + 1 in [27] + [83]	~ 200	233–299	1.5–14.0	0.25–0.99
CO <sub>2</sub> -SO <sub>2</sub>	3	0	1 in [8]+[84, 85]	~ 425	293–418	2.1–9.5	0.09–0.93
CO <sub>2</sub> -H <sub>2</sub> S	8	3	2 in [8] + [86–91]	> 270	248–365	1.0–8.9	0.01–0.97
CO <sub>2</sub> -N <sub>2</sub> O	1	0	1 in [8]	> 100	293–307	5.3–7.2	0.26–0.88
CO <sub>2</sub> -NO <sub>2</sub> / CO <sub>2</sub> -N <sub>2</sub> O <sub>4</sub>	2	1	1 in [8] + [92]	26	262–328	0.17–9.0	0.005–0.88
CO <sub>2</sub> -CO	3	1	1 in [8] + 1 in [27] + [93]	106	223–293	0.8–14.2	0.20–0.996
CO <sub>2</sub> -H <sub>2</sub>	8	4	2 in [8] + [64, 71, 79, 80, 94, 95]	> 400	218–303	0.9–172	0.07–0.999
CO <sub>2</sub> -CH <sub>4</sub>	19	15	9 in [8] + [74, 75, 96–103]	> 180	153–320	0.68–48	0.026–0.99
CO <sub>2</sub> -H <sub>2</sub> O	>50		Eg. 41 refs. in [27]	>1500	251–623	0.1–350	0.08–1.00
CO <sub>2</sub> -NH <sub>3</sub>	2	0	2 in [8]	62	413–531	4.3–81.7	0.023–0.33
H <sub>2</sub> O-N <sub>2</sub>	29	15	26 in [27] + [104–106]	> 876	233–657	0.045–270	0.01–1.00
H <sub>2</sub> O-O <sub>2</sub>	9	5	5 in [27] + [107–110]	246	273–711	0.1–280	0.00–0.99
H <sub>2</sub> O-Ar	12	10	9 in [27] + [111–113]	> 460	258–663	0.1–340	0.00–0.95
H <sub>2</sub> O-SO <sub>2</sub>	30	8	23 in [56] + [114–120]	> 756	273–423	2·10 <sup>-4</sup> –345	0.86–0.999
H <sub>2</sub> O-H <sub>2</sub> S	17	6	13 in [58] + [121–124]	> 700	273–589	0.01–20.7	5·10 <sup>-4</sup> –0.9997
H <sub>2</sub> O-N <sub>2</sub> O	3	2	[125–127]	> 52	286–303	0.1–7.3	0.95–0.9996
H <sub>2</sub> O-CO	2	2	[122, 128]	41	304–589	1.1–13.8	0.001–0.99995
H <sub>2</sub> O-H <sub>2</sub>	6	5	[122, 129–133]	> 25	310–713	0.34–250	6·10 <sup>-4</sup> –0.99996
H <sub>2</sub> O-CH <sub>4</sub>	This system is nominally well covered, for instance with more than 30 sources found in [54]						
H <sub>2</sub> O-MEA	These systems are nominally relatively well covered, see [54, 134]						
H <sub>2</sub> O-DEA							
H <sub>2</sub> O-MDEA							
H <sub>2</sub> O-NH <sub>3</sub>							
CO <sub>2</sub> -N <sub>2</sub> -O <sub>2</sub>	3	0	2 in [8] + 1 in [27]	80	218–273	5.1–13	–0.925
CO <sub>2</sub> -N <sub>2</sub> -H <sub>2</sub>	1	1	[80]	36	253–302	2.1–8.7	0.95–0.93
CO <sub>2</sub> -CO-H <sub>2</sub>	1	1	1 in [8]	36	233–283	2–20	0.17–0.98
CO <sub>2</sub> -CH <sub>4</sub> -N <sub>2</sub>	2	2	2 in [8]	> 100	220–293	6–10	0.27–0.99
CO <sub>2</sub> -CH <sub>4</sub> -H <sub>2</sub> S	1	0	1 in [8]	16	222–239	2.1–4.8	0.024–0.78
CO <sub>2</sub> -H <sub>2</sub> O-CH <sub>4</sub>	5	5	[38, 135–138]	> 132	243–423	0.1–100	0.001–0.83
CO <sub>2</sub> -H <sub>2</sub> O-NaCl	16 15 10 in [62]+[62, 139–143]						
CO <sub>2</sub> -brines							
CO <sub>2</sub> -O <sub>2</sub> -Ar-N <sub>2</sub>	1	1	[144]	5	252–293	7.1–9.0	0.892

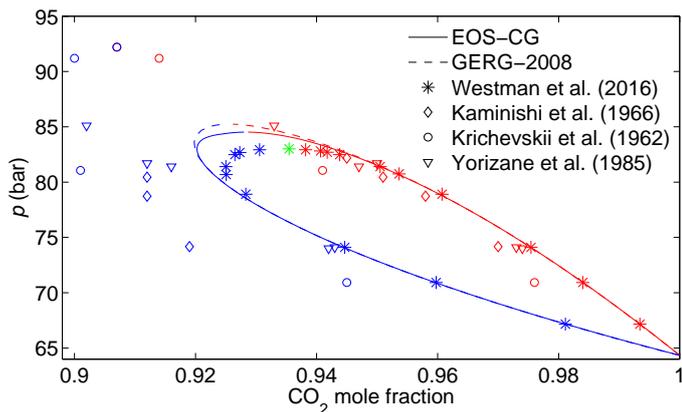


Figure 1: Data situation for CO<sub>2</sub>-N<sub>2</sub> VLE around 298.15 K. Experimental data from [64–67] are plotted with the GERG-2008 [68] and EOS-CG [27] models. Bubble points are shown in red, dew points in blue, and a supercritical measurement from the measurement campaign reported in [65] is shown in green.

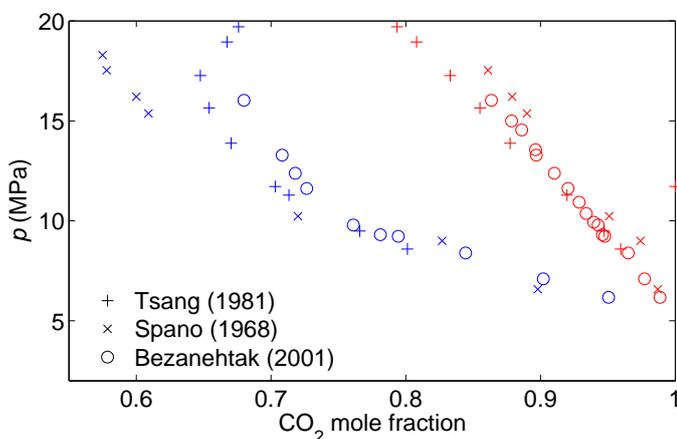


Figure 2: Available data for CO<sub>2</sub>-H<sub>2</sub> VLE. All data at (290.00 ± 0.15) K. Data from [69–71]. Bubble points are shown in red and dew points in blue.

recent measurements [79, 80]. That an improvement was much needed despite the presence of literature data is illustrated in Figure 2. For CO<sub>2</sub>-Ar there is one recent data set which seems to be of high quality [145], but the region around the critical locus is not well covered. For the other primary mixtures listed, the data situation is generally poor. For CO<sub>2</sub>-SO<sub>2</sub> for instance, there are many data points, but most of the data are from a single author around the year 1902, and the latest data are from 1931. For CO<sub>2</sub>-NO<sub>x</sub> and CO<sub>2</sub>-CO there are big gaps in the data. No VLE data have been found for the binary systems CO<sub>2</sub>-COS, CO<sub>2</sub>-NO, or CO<sub>2</sub>-amines / CO<sub>2</sub>-NH<sub>3</sub>.

In order to avoid corrosion, it is of high importance to accurately determine the threshold for the formation of a water-rich liquid phase, and hence also VLE measurements on binary mixtures between water and the other impurities have been included in Table 2. Also here the amount of data varies significantly. It should be noted that a large part of the data are on gas solubility in water. For H<sub>2</sub>O-SO<sub>2</sub> and H<sub>2</sub>O-H<sub>2</sub>S, a large fraction of the data is very old, in the case of H<sub>2</sub>O-SO<sub>2</sub>, 16 of the sources were published before 1940, the first one in 1855. Again the coverage

of e.g. CO and NO<sub>x</sub> seems poor, and no data have been found for binary mixtures between H<sub>2</sub>O and COS, NO and NO<sub>2</sub>/N<sub>2</sub>O<sub>4</sub>.

For completeness, also multicomponent CO<sub>2</sub> mixtures have been included in Table 2. Perhaps the most interesting systems here are CO<sub>2</sub>-H<sub>2</sub>O-NaCl and CO<sub>2</sub>-brines, for which there are some data to be studied, and which are relevant for injection and storage. Ternary mixtures between CO<sub>2</sub>, H<sub>2</sub>O, and amines or NH<sub>3</sub>, which are seen as more important for some capture processes than for transport and injection, have not been included in Table 2, but some data have been identified.

### 2.2.2. Vapour-liquid-liquid equilibrium (VLLE)

Some of the primary mixtures, like methane and CO<sub>2</sub> and water and CO<sub>2</sub>, are known to form immiscible liquids at certain conditions, i.e., vapour-liquid-liquid equilibrium (VLLE). Again, it is of considerable practical interest to accurately characterize when a water-rich liquid phase forms. As seen in Table 3, the experimental data found for this kind of systems are scarce.

### 2.2.3. Equilibria involving solids and hydrates

In Table 4, the relevant phase equilibrium measurements found for systems involving solids are listed. During depressurization, the temperature of dry CO<sub>2</sub> mixtures could drop significantly, facilitating the formation of solid CO<sub>2</sub> (dry ice). New equilibria models for pure CO<sub>2</sub> with solids have recently been developed [169, 170], although, as stated in [170], the amount of thermodynamic data on solid CO<sub>2</sub> is very limited. For CCS, it is of interest to quantify also the change in freezing point due to impurities. For most impurity components, we would expect a freezing point depression. As seen in Table 4, very few measurements have been performed with such systems, except for CO<sub>2</sub> mixed with CH<sub>4</sub> or N<sub>2</sub>. For these mixtures, the main focus has, however, been on low temperatures and hence relatively low CO<sub>2</sub> concentrations in the fluid phase(s), and the measurements on CO<sub>2</sub>-N<sub>2</sub> are mostly quite old and incomplete.

With water involved, solid or hydrate phases can be introduced at much higher temperatures. Quite a bit of data have been found for the binary CO<sub>2</sub>-H<sub>2</sub>O system. With additional components present, far less data are available, and for the systems that are covered, a significant part of the data comes from a single source [63].

### 2.2.4. Density and related properties

Available data found for density and the related properties virial coefficients and compressibility are shown in Table 5. At first glance, density seems to be relatively well covered for a number of the primary binary mixtures, such as CO<sub>2</sub>-N<sub>2</sub>, CO<sub>2</sub>-Ar, CO<sub>2</sub>-CH<sub>4</sub>, and CO<sub>2</sub>-H<sub>2</sub>O, but approximately 99 % of the data points for CO<sub>2</sub>-CO and 80 % of the data points on CO<sub>2</sub>-CH<sub>4</sub> come from the same experimental setup, all with a mole fraction of 0.97 CO<sub>2</sub> or more [93, 189]. It should also be noted that density measurements have an added degree of freedom as the composition of the fluids can be varied, in contrast to phase equilibria measurements of binary mixtures where the composition of each phase at a given temperature and pressure is fixed. Furthermore, it should be noted that for CO<sub>2</sub>-H<sub>2</sub>O, most data are for low CO<sub>2</sub> content, and no data have been found below

Table 3: VLLE equilibrium data for CCS-relevant systems.

System (1)-(2)	# Sources		Location of References	# Points	$T$ (K)	Data ranges	
	Total	1975→				$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub> -H <sub>2</sub> O	3	3	2 in [27] + [146]		278–313	6.4–29.5	
H <sub>2</sub> O-H <sub>2</sub> S	2	1	[121, 124]	> 15	311–373	4–20.7	0.018–0.95
H <sub>2</sub> O-N <sub>2</sub> O	2	1	[121, 146]				
CO <sub>2</sub> -H <sub>2</sub> O-CH <sub>4</sub>	1	1	[138]	37	293–301	6.5–7.7	4·10 <sup>-5</sup> –0.22

Table 4: Phase equilibrium data involving solids and hydrates for CCS-relevant systems.

System	# Sources		Location of References	# Points	$T$ (K)	Data ranges	
	Total	1975→				$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub> -N <sub>2</sub>	6	2	[79, 94, 147–150]	> 16	140–190	4.8–200	
CO <sub>2</sub> -O <sub>2</sub>	1	1	[151]	12	91–119	0.4–0.4	4·10 <sup>-6</sup> –10 <sup>-5</sup>
CO <sub>2</sub> -SO <sub>2</sub>	1	0	[152]			0.1	
CO <sub>2</sub> -H <sub>2</sub> S	1	0	[152]			0.1	
CO <sub>2</sub> -H <sub>2</sub>	1	1	[79]	3	217–218	4.3–13.7	
CO <sub>2</sub> -CH <sub>4</sub>	7	2	[153–159]		98–217	0.1–10	0.01–0.58
CO <sub>2</sub> -H <sub>2</sub> O	>50		E.g. 44 in [160]+3 in [63]+[63, 161, 162]				
CO <sub>2</sub> -H <sub>2</sub> O-N <sub>2</sub>	4	4	3 in [63]+[63]		273–289	2.1–55.1	0–1
CO <sub>2</sub> -H <sub>2</sub> O-CO	2	2	1 in [63]+[63]		273–286	1.4–21.3	0.1–0.97
CO <sub>2</sub> -H <sub>2</sub> O-H <sub>2</sub>	4	3	3 in [63]+[63]		274–287	1.6–16.5	0.19–0.97
CO <sub>2</sub> -H <sub>2</sub> O-CH <sub>4</sub>	2	10	9 in [63]+[63]		264–288	1.8–20.0	0–1
CO <sub>2</sub> -brines	4	4	[163–166]	199	259–281	0.9–28	
CO <sub>2</sub> -H <sub>2</sub> O-SO <sub>2</sub>	1	1	[167]	3	277–280	1.8–2.7	
CO <sub>2</sub> -H <sub>2</sub> O-N <sub>2</sub> -SO <sub>2</sub>	1	1	[168]	3	273–276	7.2–8.7	
CO <sub>2</sub> -H <sub>2</sub> O-NO <sub>2</sub> -O <sub>2</sub>	1	1	[167]	3	277	1.9	

Table 5: Data for density, virial coefficients and compressibility for CCS-relevant systems.

System	# Sources		Location of References	# Points	$T$ (K)	Data ranges	
	Total	1975→				$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub> -N <sub>2</sub>	37	25	6 in [8] + 24 in [27] + [63, 171–176]	>5210	208–673	–273	0.01–0.98
CO <sub>2</sub> -O <sub>2</sub>	7	2	5 in [27] + [63, 171]	377	268–423	–47.8	0.49–0.95
CO <sub>2</sub> -Ar	19	11	3 in [8] + 8 in [27] + [63, 174, 176–181]	>1480	213–573	0.1–101	0.01–0.96
CO <sub>2</sub> -SO <sub>2</sub>	3	2	1 in [8] + [84, 181]	168	287–347	0.1–20	0.13–0.97
CO <sub>2</sub> -H <sub>2</sub> S	6	4	1 in [8] + [182–186]	>900	220–501	0.1–60.5	0.5–0.94
CO <sub>2</sub> -N <sub>2</sub> O	1	1	[187]	42	238–358	1–5.9	0.09–0.91
CO <sub>2</sub> -CO	9	7	1 in [8] + 3 in [27] + [63, 93, 174, 188, 189]	> 50000	223–423	0.1–48.6	0.29–0.996
CO <sub>2</sub> -H <sub>2</sub>	11	7	[63, 71, 171, 174, 190–196]	>632	223–473	0.05–50.7	0.22–0.98
CO <sub>2</sub> -CH <sub>4</sub>	22	19	5 in [8]+[63, 75, 100, 174, 189, 191, 194, 197–206]	>6250	206–573	0.08–100	0.01–0.996
CO <sub>2</sub> -H <sub>2</sub> O	35	29	21 in [27] + 10 in [61] + [207–210]	>3619	273–1023	–600	0.001–0.997

273.25 K, although data for low H<sub>2</sub>O concentrations and below 273.25 K would be highly relevant for CCS. Most of the data for CO<sub>2</sub>-O<sub>2</sub> are old, and have a limited concentration range. For CO<sub>2</sub>-SO<sub>2</sub> most of the data are from 1901 [84], and about 94 % of the data points for CO<sub>2</sub>-H<sub>2</sub>S are from a single source [186]. No data have been found for CO<sub>2</sub>-COS, CO<sub>2</sub>-NO, CO<sub>2</sub>-NO<sub>2</sub> or CO<sub>2</sub>-N<sub>2</sub>O<sub>4</sub>, or CO<sub>2</sub>-amines or CO<sub>2</sub>-NH<sub>3</sub> for these important properties.

### 2.2.5. Speed of sound

Perhaps due to the high attenuation of acoustic waves in CO<sub>2</sub>, there is not a lot of speed-of-sound data available. Hence also pure CO<sub>2</sub> is included in the speed-of-sound data overview of Table 6. For mixtures, there is only limited-range data available for CO<sub>2</sub>-N<sub>2</sub>, CO<sub>2</sub>-Ar, and CO<sub>2</sub>-H<sub>2</sub>O. Except for CO<sub>2</sub>-N<sub>2</sub> and CO<sub>2</sub>-H<sub>2</sub>O, all the liquid mixture speed-of-sound data come from a single source [63]. The claimed uncertainty of Al-Siyabi [63] is 1 m s<sup>-1</sup>, but no uncertainty analysis is provided, and data is only provided for a single composition per binary system. For a number of the primary mixtures, no liquid and / or vapour speed-of-sound measurements have been found. The few measurements found for CO<sub>2</sub>-H<sub>2</sub>O are not in a relevant range for CO<sub>2</sub> transport and storage.

### 2.2.6. Viscosity

The identified viscosity data for pure CO<sub>2</sub> and primary binary mixtures relevant for CCS are summarized in Table 7. The available data in the 80s and 90s for pure CO<sub>2</sub> were reviewed in [57, 59, 60]. In the modelling work of Vesovic *et al.* [59], the liquid data had all to be abandoned because of their inconsistencies, and a data-based reference model for the liquid phase could only be made once new measurements were available eight years later [60]. Works prior to 1957 were discarded due to inaccurate working equations. It should be noted that since the work of Fenghour and Wakeman [60], Vogel reportedly [230, 235] has reevaluated measurements from the 80s and 90s [236, 237] using accurate ab-initio correlations for helium. The data situation for viscosity is relatively thin for pure CO<sub>2</sub> but much worse for mixtures. For five binary systems, CO<sub>2</sub>-O<sub>2</sub>, CO<sub>2</sub>-Ar, CO<sub>2</sub>-CO, CO<sub>2</sub>-H<sub>2</sub>, and CO<sub>2</sub>-CH<sub>4</sub>, all liquid data are again provided by Al-Siyabi [63] for a single composition per system, using a single capillary viscometer. The uncertainty is claimed to be 1 %, with only uncertainty contributions from pressure measurements considered. No liquid viscosity data have been found for an important binary system such as CO<sub>2</sub>-N<sub>2</sub>. For CO<sub>2</sub>-H<sub>2</sub>O, only liquid-phase measurements on water-rich mixtures are available. For gas phase, there are a few more sources, but many of the measurements are quite old. No data have been found for either liquid or vapour/supercritical phase for CO<sub>2</sub>-H<sub>2</sub>S, CO<sub>2</sub>-COS, CO<sub>2</sub>-NO, CO<sub>2</sub>-NO<sub>2</sub>, CO<sub>2</sub>-N<sub>2</sub>O<sub>4</sub>, CO<sub>2</sub>-amines, or CO<sub>2</sub>-NH<sub>3</sub>.

### 2.2.7. Thermal conductivity

Like for viscosity, the data situation for thermal conductivity for CCS mixtures is highly unsatisfactory. The data available for pure CO<sub>2</sub> and binary mixtures between CO<sub>2</sub> and impurities of CCS are shown in Table 8. A relatively high number of sources are found for pure CO<sub>2</sub>. However, when analysing the data in

order to set up a model for thermal conductivity of pure CO<sub>2</sub>, Vesovic *et al.* [59] discarded most of the data sources and had to use theoretical predictions in the liquid-phase and high temperature zero-density regions. Only a limited number of data sets have been published since, but a new set of measurements from [235] appears to be fairly complete. Except for CO<sub>2</sub>-H<sub>2</sub>O, no liquid-phase mixture data have been found, and only a handful of modern measurements for the vapour or supercritical phase are available for mixtures.

## 3. Thermophysical property models

In this section, we briefly review models and methods for calculating the thermophysical properties of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures. Highly relevant topics, such as implementation in fluid-dynamic models, and methods for calculating flow through restrictions, are also covered.

### 3.1. Property models for pure CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures

During transport by pipeline or ship, the CO<sub>2</sub>-rich fluid is normally in equilibrium. However, equilibrium properties are also needed as a useful starting point for non-equilibrium models. The thermodynamic properties of pure CO<sub>2</sub> are well described by the Span-Wagner EOS [243]. The Span-Wagner EOS is very accurate when it comes to prediction of density and saturation line. The estimated uncertainty for density predictions in the pressure and temperature domain relevant for transport of CO<sub>2</sub> is 0.05 %. The uncertainty in vapour pressure predictions is 0.006 %. Speed of sound and isobaric heat capacity are reported to be within 1.0 % and 1.5 %, respectively. In order to describe dry-ice in equilibrium with liquid and vapour, an auxiliary model is required. Trusler [169] developed a Helmholtz free energy model, and Jäger and Span [170] developed a Gibbs free energy model, that can be used to describe solid-liquid-vapour equilibrium for pure CO<sub>2</sub> and mixtures containing CO<sub>2</sub> in combination with a model for the fluid CO<sub>2</sub>. Considering only pure CO<sub>2</sub>, the auxiliary equations for the sublimation line published by Span and Wagner [243], have been used together with the Clausius-Clapeyron equation to describe vapour-solid equilibrium [244]. This approach is, however, not as easily extendable to CO<sub>2</sub>-rich mixtures.

The Span-Wagner formulation is CPU demanding to solve compared to simpler models, like the commonly used Peng-Robinson (PR) EOS [245]. To address this, a new EOS for pure CO<sub>2</sub> has been developed by Demetriades *et al.* [246]. The EOS is designed for accuracy between 0 °C and the critical temperature of CO<sub>2</sub>. The pressure of interest is set to be below 150 bar. This pressure-explicit EOS is relatively fast to evaluate, and it gives significant predictive improvements over Peng-Robinson, and contains much fewer parameters than the Span-Wagner EOS. How the Demetriades *et al.* [246] EOS performs compared to other alternatives, e.g. the modified Benedict-Webb-Rubin (MBWR) EOS [247], is unknown. The accurate technical equations of state for CO<sub>2</sub> used in GERG-2004 [248], also represent a less CPU-demanding alternative to the Span-Wagner reference EOS. Demetriades and Graham [249] extended the pure-fluid

Table 6: Speed-of-sound data for CCS-relevant systems.

System	Vap/ Liq	# Sources		Location of References	# Points	Data ranges		
		Total	1975→			$T$ (K)	$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub>	V	6	4	[202, 211–215]	> 445	220–450	0.22–14.2	1
	L	5	2	[63, 216–219]	> 484	248–473	3.6–450	1
CO <sub>2</sub> -N <sub>2</sub>	V	1	1	1 in [27]	65	250–350	0.5–10.3	0.5
	L	2	2	[63, 220]	79	268–423	9.5–400	0.40–0.96
CO <sub>2</sub> -O <sub>2</sub>	L	1	1	[63]	62	268–301	8.9–41	0.94
CO <sub>2</sub> -Ar	V	1	1	[221]	30	275–500	< 8	0.50–0.75
	L	1	1	[63]	62	268–301	8.93–41	0.93
CO <sub>2</sub> -CO	L	1	1	[63]	61	268–301	9.71–41.1	0.96
CO <sub>2</sub> -H <sub>2</sub>	L	1	1	[63]	57	268–301	9.71–40.8	0.95
CO <sub>2</sub> -CH <sub>4</sub>	L	1	1	[63]	61	268–301	8.87–38.2	0.95
CO <sub>2</sub> -H <sub>2</sub> O	V	1	1	[222]		281–297	0.1	
	L	1	1	[223]	27	293–575	570–6000	0.05
CO <sub>2</sub> -Ar-CO	L	1	1	[63]	58	268–301	10.3–41.2	0.97
CO <sub>2</sub> -Ar-CO	L	1	1	[63]	58	268–301	10.3–41.2	0.97
CO <sub>2</sub> -CH <sub>4</sub> -H <sub>2</sub> -N <sub>2</sub>	L	1	1	[63]	60	268–301	7.6–40.6	0.95

Table 7: Viscosity data for CCS-relevant systems.

System	Vap/ Liq	# Sources		Location of References	# Points	Data ranges		
		Total	1975→			$T$ (K)	$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub>	V	39	18	26 in [57, 59, 60] + [215, 224–230]	> 1150	202–1871	0.02–8000	1
	L	34		28 in [59] + 7 in [60]		220–543	0.6–350	1
CO <sub>2</sub> -N <sub>2</sub>	V	5	0	5 in [9]	150	289–873	0.1–120	0–1
	V	2	1	2 in [9]	24	297–673	0.1	0–1
CO <sub>2</sub> -O <sub>2</sub>	L	1	1	[63]	60	280–343	9.1–47.3	0.95
	V	4	2	3 in [9] + [231]	198	213–673	0.02–2.5	0–0.92
CO <sub>2</sub> -Ar	L	1	1	[63]	48	280–343	7.8–50.4	0.95
	V	3	0	3 in [9]	69	238–353	0.1	0–1
CO <sub>2</sub> -SO <sub>2</sub>	V	3	1	2 in [9] + [232]	> 34	298–550	0.1	0–1
CO <sub>2</sub> -N <sub>2</sub> O	V	1	1	1 in [9]	10	298–473	0.1	0.31&0.77
	L	1	1	[63]	56	280–343	8.9–49.4	0.95
CO <sub>2</sub> -H <sub>2</sub>	V	6	2	6 in [9]	65	291–1100	0.1–0.3	0–1
	L	1	1	[63]	51	280–343	8.7–45.4	0.95
CO <sub>2</sub> -CH <sub>4</sub>	V	5	1	4 in [9] + [233]	406	293–673	0.1–172	0–1
	L	1	1	[63]	52	280–343	6.5–50.1	0.95
CO <sub>2</sub> -H <sub>2</sub> O	V	1	0	1 in [9]	8	303	0.1	0.96–0.99
	L	8	5	5 in [9] + [210, 234]	175	273–449	0.1–100	0.003–0.030
CO <sub>2</sub> -H <sub>2</sub> O-NaCl	L	2	2	2 in [9]	90	273–278	0.1–30	0–0.016

Table 8: Thermal conductivity data for CCS-relevant systems.

System	Vap/ Liq	# Sources		Location of References	# Points	Data ranges		
		Total	1975→			$T$ (K)	$p$ (MPa)	$x_{\text{CO}_2}$
CO <sub>2</sub>	V/L	65	12	60 in [59] + [235, 238–242]		186–2000	–2000	1
CO <sub>2</sub> -N <sub>2</sub>	V	10	1	10 in [9]	257	273–1033	0.1–300	0–1
CO <sub>2</sub> -O <sub>2</sub>	V	1	0	1 in [9]	4	369 & 370		0.22–0.73
CO <sub>2</sub> -Ar	V	3	2	3 in [9]	270	273–473	0.1–11.3	0–1
CO <sub>2</sub> -SO <sub>2</sub>	V	1	0	1 in [9]	9	323 & 373		0.1–0.90
CO <sub>2</sub> -N <sub>2</sub> O	V	2	1	2 in [9]	90	300.65–723	0.1–4.25	0–1
CO <sub>2</sub> -H <sub>2</sub>	V	7	1	7 in [9]	120	258–893	0.1–7.5	0–1
CO <sub>2</sub> -CH <sub>4</sub>	V	4	3	3 in [9] + [240]	390	228–433	0.1–17.7	0.075–0.88
CO <sub>2</sub> -H <sub>2</sub> O	V/L	4	0	3 in [9]	41	298–603	0.1	0–1

EOS [246] with mixture rules to describe the binaries CO<sub>2</sub>-H<sub>2</sub>, CO<sub>2</sub>-O<sub>2</sub> and CO<sub>2</sub>-N<sub>2</sub> with good agreement with experimental data.

Analogous to the GERG equations for description of natural gas with impurities, EOSs are being developed for combustion gases (CG), where CO<sub>2</sub> is the main component. EOS-CG [27, 250, 251] is based on a single-component reference equation for Helmholtz free energy in the natural variables temperature and density/volume. In contrast to GERG-2004/2008, the single-component reference EOS is used, and not a simplification. I.e. for pure CO<sub>2</sub>, EOS-CG becomes the Span-Wagner EOS. If the binary interaction parameters are correlated to accurate measurements, especially in the critical region, the use of accurate pure-fluid EOSs will give an improvement over GERG. In order to describe mixtures, Helmholtz free energy mixing rules are used [252–255]. Improved binary mixture models and parameters have been developed so far for the exhaust-gas components CO<sub>2</sub>, H<sub>2</sub>O, N<sub>2</sub>, O<sub>2</sub>, Ar and CO. One challenge with mixtures is the extrapolation of the pure-fluid reference equations. A species may exist in a mixture phase where the pure fluid is unstable, and therefore not tuned to experimental data. Despite some difficulties, good results have been published, and significant improvement over GERG-2008 is seen for mixtures containing CO<sub>2</sub> and H<sub>2</sub>O [27].

Wilhelmsen *et al.* [256] compared density predictions for pure CO<sub>2</sub> and CO<sub>2</sub> mixtures, using five EOSs. Soave-Redlich-Kwong (SRK) [257] (with and without Péneloux shift [258]), Lee-Kesler [259], Peng-Robinson [245], GERG-2004, and SPUNG [260] were evaluated against the Span-Wagner EOS and experimental data. Wilhelmsen *et al.* focused on an extended corresponding state approach, termed SPUNG. SPUNG uses SRK and classical van der Waals mixing rules to scale a reference EOS. Here the MBWR equation [261] for propane was used. The extended corresponding state approach was found to be an excellent compromise between computational speed and accuracy.

Statistical Associating Fluid Theory (SAFT) [262, 263] models are popular for many application, and are also of interest for CCS fluid mixtures. Diamantonis *et al.* [264] compared SAFT and Perturbed-Chain SAFT (PC-SAFT) [265] with cubic EOSs, Redlich-Kwong (RK) [266], SRK and PR, and assessed the vapour-liquid equilibrium modelling capabilities for CO<sub>2</sub> binary and ternary mixtures. For the impurities CH<sub>4</sub>, N<sub>2</sub>, O<sub>2</sub>, SO<sub>2</sub>, Ar and H<sub>2</sub>S, it was concluded that the SAFT, PC-SAFT, RK, SRK and PR are of comparable accuracy when binary interaction parameters are fitted to experimental data. In this case, there is little benefit of using the more complex and more CPU demanding SAFT and PC-SAFT models over cubic EOSs. In Diamantonis *et al.* [264], H<sub>2</sub>S was the only component considered as associating when using SAFT, but no components were treated as associating with PC-SAFT, as this gave the best fit to experimental data. SAFT and PC-SAFT are expected to perform better than cubic EOSs in systems with components which are more strongly associating than H<sub>2</sub>S, such as H<sub>2</sub>O.

There has also been an effort to combine SAFT-based EOSs with molecular-dynamics simulations [267]. By tuning pure-fluid saturation data to SAFT- $\gamma$ , force field parameters can be

established [268]. These parameters are used in coarse-grained molecular dynamics simulations, allowing for predictions of other properties, like interfacial tension. The model was extended to binary and ternary mixtures by Lobanova *et al.* [269], and good agreement with experimental data was observed for low-pressure data. As for many of the SAFT-based models, the pure-fluid critical points were overestimated, something which also leads to poor correlation in the critical region for mixtures. For CO<sub>2</sub>, the critical point is close to the operational area for pipeline transport, making good predictions in this region important. The critical point must therefore be accounted for when tuning parameters used for pure-fluid description with SAFT. Herdes *et al.* [270] have developed a new parameter set for the SAFT- $\gamma$  model, for CO<sub>2</sub> and other components, using the pure-fluid critical point explicitly. These parameters potentially improve the prediction of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures in the critical region.

Cubic EOSs can predict VLE quite well, but are known for poor density predictions in the liquid phase and in the critical region. Li and Yan [271] also found SRK to predict VLE properties in CO<sub>2</sub> mixtures satisfactorily. In process modelling, the poor density predictions can to some extent be overcome using density corrections. Using a three-parameter EOS might also give improved density predictions [272]. For fast transients in pipelines, where also the speed of sound comes into play, a density correction is not sufficient. In this case, the more detailed modelling approach of EOS-CG/GERG is far superior [39], as these systems have been tuned to both density and speed-of-sound experimental data.

For EOS-CG, the CO<sub>2</sub> and H<sub>2</sub>O system has been extended to include hydrate formation [160]. Early work was performed by Chapoy *et al.* [273] measuring and modelling hydrate temperatures in CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures. Later, Chapoy *et al.* [274] used the Cubic-Plus-Association [275] method to describe the fluid chemical potentials and the solid solution theory of van der Waals and Platteeuw [276] to describe the hydrate phase appearance in CO<sub>2</sub>-rich mixtures. Very few data sets are identified for CO<sub>2</sub>-hydrate formation under saturated conditions. Chapoy *et al.* therefore saw a need for more experiments in order to improve the thermodynamic modelling of CO<sub>2</sub>-hydrate systems. Duan and Sun [277] modified a van der Waals and Platteeuw model for CO<sub>2</sub>-hydrate prediction, and obtained good agreement with experimental data. To describe the fluid phases, an ab initio quantum chemical method was used. The water activity was corrected using the Pitzer model to account for the presence of electrolytes.

Viscosity of pure CO<sub>2</sub> for conditions relevant for transport and capture is described using the correlation of Fenghour and Wakeman [60] to an accuracy below 2%. In the low-pressure area, the viscosity predictions are much better. This is also confirmed by recent experiments, but Schäfer *et al.* [230] saw room for improvements in the models. Thermal conductivity of pure CO<sub>2</sub> is correlated to a similar degree of accuracy by Vesovic *et al.* [59]. New models which are claimed to better predict e.g. the critical enhancement, i.e. behaviour around the critical point, have been announced for both viscosity and thermal conductivity [235].

Viscosity of mixtures can be described by the extended corresponding-principle-state approach. One such model is TRAPP [278]. TRAPP is also used for thermal conductivity modelling of mixtures [279]. Friction theory is another interesting approach [280] for viscosity predictions. Those models will be able to describe the properties of CO<sub>2</sub>-rich mixtures, but this is not documented in the public literature.

### 3.2. Implementation in fluid-dynamic models

In compressible two-phase flow models, integrated using finite volume methods, the iso-choric-iso-energetic phase-equilibrium problem must be solved, unless modelling simplifications are made. Giljarhus *et al.* [281] described a framework for solving the iso-choric-iso-energetic phase-equilibrium problem using the Span-Wagner [243] EOS. Later, Hammer *et al.* [244] extended the framework by including dry-ice at the sublimation line, using the Gibbs-Duhem equation together with an auxiliary model for the the sublimation line. Solving the EOS directly for single-component CO<sub>2</sub> depressurization has been performed by several authors [20, 244, 281–284].

For multi-component systems, the iso-choric-iso-energetic phase-equilibrium problem becomes more difficult, and an approach like the one presented by Michelsen [285] must be taken. For CO<sub>2</sub> systems, this method has successfully been used for depressurization simulations by Munkejord and Hammer [39]. Due to the time consumption solving the EOS directly during CFD simulations, the use of pre-calculated interpolation tables may be preferable. Elshahomi *et al.* [286] performed simulations of pipeline depressurizations in 2D with Fluent® using thermodynamic look-up tables.

### 3.3. Flow through restrictions

Simulation models for depressurization of pipes or valves normally require the flow through valves or restrictions to be implemented as a boundary condition. The first stages of the depressurization often involve choked flow, in which the flow velocity is restricted by the effective two-phase speed of sound. The most common way of modelling choked flow is by using a homogeneous equilibrium model (HEM), and assuming steady-state flow, thus obtaining a general Bernoulli formulation, i.e., energy and mass conservation for an isentropically expanding flow. The choking condition is found by equating the velocity of the expanding fluid with the speed of sound. A major problem of this formulation is the singularity of the triple point. The speed of sound becomes zero, as the density can change isentropically without a change in pressure [287, Sec. 2.8.1]. This is illustrated in Figure 3. Figure 3a shows an isentropic depressurization path plotted in density-entropy space. The isentrope starts from a dense liquid state, continues through the liquid-vapour two-phase area before passing through the triple point, ending at atmospheric pressure in the two-phase solid-vapour region. In Figure 3b, the homogeneous mixture speed of sound is plotted against density for the same isentropic path. It is seen that the speed of sound is discontinuous at all phase boundaries.

Martynov *et al.* [288] described a choke model following the HEM principle, handling the triple point by maximizing mass

flux as a function of dry-ice mass fraction ( $x_s$ ) in the triple point. This is equivalent to using the mass flux found at the triple point entry from the liquid-vapour region, ( $x_s = 0$ ). The model was subsequently applied for simulating experiments of CO<sub>2</sub> release from a pipeline [289].

Martynov *et al.* [290] modelled the dry ice in equilibrium with pure CO<sub>2</sub> with an extended Peng-Robinson approach. Three different parameter sets for the cubic EOS were used; one for liquid and vapour, one for the melting line and the properties of dry ice in equilibrium with liquid, and one for the sublimation line and the properties of dry ice in equilibrium with vapour. It is unclear whether this gave consistent properties of dry ice in the triple point. Given the development of a Gibbs free energy function [170], and a Helmholtz free energy function for dry ice [169, 291], cubic equations of state can be coupled directly with the dry-ice models. This has found an application in the modelling of supersonic separation of CO<sub>2</sub> from an exhaust gas [292].

## 4. Pipeline transport of CO<sub>2</sub>

Some challenges related to CO<sub>2</sub> transport in pipes, such as enlarged two-phase region, free water, etc., increase with an increasing amount of impurities in the CO<sub>2</sub>. On the other hand, the removal of impurities at the capture plant entails increased investment and operational costs. This constitutes a techno-economic optimization problem which has to be considered for each specific project. Some of the data and models needed to perform detailed studies are yet lacking.

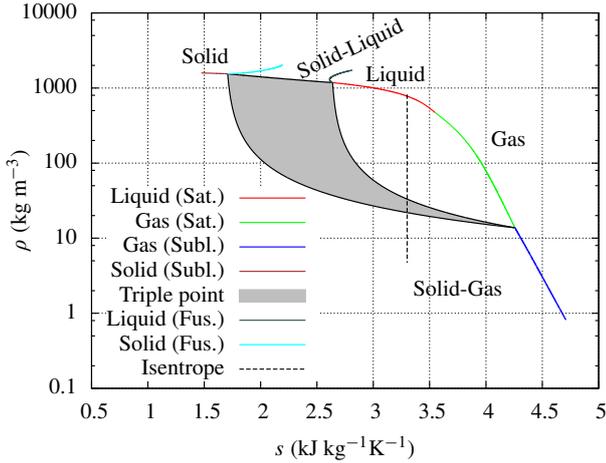
For CO<sub>2</sub>-transport pipelines operating in a single-phase state, several quantities, such as pressure drop and pump or compressor work, can be estimated if sufficiently accurate thermodynamic and transport property models are available. It should be noted that CO<sub>2</sub> mixtures from different capture technologies will have different dynamic behaviour in pipelines [13]. An important issue is also the effect of impurities on corrosion [293].

Here we will concentrate on transient two-phase flow effects, which need to be accounted for during design and operation of CO<sub>2</sub>-transport pipeline networks.

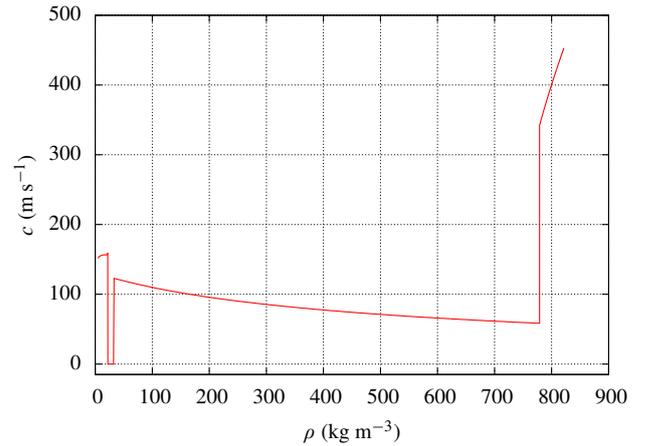
### 4.1. Pipe depressurization

The depressurization of a pipe filled with CO<sub>2</sub> constitutes a relatively well defined case, and it is suitable for model validation for several reasons. First, the pressure-wave propagation during depressurization needs to be understood due to its application to fracture-propagation control. Second, transient flow-model formulations have inherent wave-propagation velocities, which ought to agree with the experimental observations, something which is particularly challenging in the two-phase region. Third, models predicting CO<sub>2</sub> dispersing in the atmosphere due to a leak, are dependent on a realistic specification of the outflow state of the pipe.

The thermo- and fluid dynamics of pipe depressurizations are tightly intertwined. As an example, both CO<sub>2</sub>-mixture composition and phase slip influence the pressure-propagation velocity [10]. Based on a homogeneous equilibrium pipeline decompression model, Brown *et al.* [294] performed a global sensitivity



(a) Density-entropy phase map for CO<sub>2</sub>.



(b) CO<sub>2</sub> equilibrium speed of sound for the isentrope drawn in Figure 3a.

Figure 3: Illustration of the speed of sound along an isentrope ( $3.3 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ) starting in a dense liquid state at 12.5 MPa, 29 °C and passing the triple point. The plots are made using the Span and Wagner [243] EOS together with the dry-ice model of Jäger and Span [170].

analysis of the impact of impurities on CO<sub>2</sub> pipeline failure, and found that the outflow rate is highly sensitive to the composition during the early stages of depressurization, where the effect of the impurities on phase equilibrium has a significant impact on the outflow.

Experimental facilities where pressure and temperature are dynamically recorded along a tube or pipe after one end of the tube is opened to the atmosphere, are commonly referred to as ‘shock tubes’ or ‘expansion tubes’. We prefer the latter designation, since, for such an experimental set-up, the shock will appear outside the tube.

As shown in Table 9, pipe-depressurization data for CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures are relatively scarce in the literature. Here we have included studies at least giving pressure as a function of time. In the table,  $l$  and  $d$  denote tube length and inner diameter, respectively.

de Koeijer *et al.* [37] compared pressure-temperature plots of measured data of a tube depressurization and model predictions using OLGA<sup>®</sup> [302, 303] employing the Span and Wagner [243] EOS. It was noted that there is room for model improvement.

Clausen *et al.* [298] measured pressure and temperature at the outlets during the depressurization of a 50 km long 24” buried onshore pipeline filled with almost-pure CO<sub>2</sub>. The case was also simulated using OLGA<sup>®</sup>, again employing the Span and Wagner [243] EOS. Good agreement was obtained for the pressure, while some discrepancies were observed for the temperature. Since the pipeline was only instrumented at the outlets, and because of some uncertainty regarding the initial conditions, clear conclusions regarding the reason for the disagreement could not be reached. Clausen *et al.* mentioned several possible reasons: The effect of impurities not being accounted for, incorrectly estimated mass-transfer rate during phase transition, incorrect flow-regime prediction, and uncertainties in the modelling of heat transfer to the surroundings.

Huh *et al.* [304] considered a tube of length 51.96 m and inner diameter 3.86 mm. See also Cho *et al.* [305]. Pressure and temperature were measured during depressurization of pure

CO<sub>2</sub> and CO<sub>2</sub>-N<sub>2</sub> mixtures with up to 8 % N<sub>2</sub>. The experimental data were compared to simulations performed using OLGA<sup>®</sup>. Rather larger discrepancies were seen than what was observed by Clausen *et al.* [298]. The experiments of Huh *et al.*, were, however, carried out in a much smaller tube and lasting 40 s instead of 10 h.

Tu *et al.* [306] conducted a somewhat different study, in which a 23 m long tube loop with an inner diameter of 3 cm filled with CO<sub>2</sub> was depressurized through nozzles of diameter 1 mm to 5 mm. The main focus was the temperature development in the leakage jet as a function of initial pressure and nozzle size.

Botros *et al.* [296] discussed an experiment designed to measure and study the decompression wave speed, which is the velocity of the rarefaction wave propagating into a pipeline, after the bursting of a disc. A specialized expansion tube with a smooth inner surface was employed, to be more representative for larger industrial pipes. Further details of the experimental facility are given in Botros [307]. The CO<sub>2</sub>-CH<sub>4</sub> mixture studied was chosen to be relevant for EOR. The single-phase speed of sound predicted by the GERG-2008 EOS was found to agree very well with the experiment, although the measured plateau pressure was found to be slightly higher than predicted using GERG-2008. This is an important aspect when it comes to designing pipelines to arrest ductile fracture. Based on the present state of knowledge of pipeline ductile fracture of CO<sub>2</sub> mixtures with impurities, Botros *et al.* recommended at least one or two full-scale burst tests for each design case.

Mahgerefteh *et al.* [308] studied measured and predicted decompression-wave speed for CO<sub>2</sub> and CO<sub>2</sub> mixtures where the initial state was gaseous. For the cases tested, it was observed that impurities in the CO<sub>2</sub> stream lowered the phase-transition pressure plateaux. This is the reverse of what is observed for depressurizations from a dense phase, see below.

Cosham *et al.* [299] studied the decompression behaviour of CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures in the dense phase. An expansion tube of length 144 m and inner diameter 146 mm was employed. Decompression curves were shown for several experiments, but

Table 9: Experimental data of CO<sub>2</sub>-pipe depressurization.

Author	Mixture (mol %)	$p$ (bar)	$T$ (°C)	$l$ (m)	$d$ (mm)	Emphasis
Armstrong and Allason [295]	CO <sub>2</sub>	98.4–105.0	6.0–13.7	200	50	$p$ & $T$ , release rate, dispersion
Botros <i>et al.</i> [296]	72.6 % CO <sub>2</sub> , 27.4 % CH <sub>4</sub>	285.7	40.5	42	38.1	Wave prop.
Brown <i>et al.</i> [297]	CO <sub>2</sub>	153.4	5.2	144	150	$p$ only
Brown <i>et al.</i> [297]	CO <sub>2</sub>	70	25.2	37	40	$p$ only
Brown <i>et al.</i> [283]	CO <sub>2</sub> (99.8 %)	36	1	256	233	$p$ & $T$
Clausen <i>et al.</i> [298]	CO <sub>2</sub> (99.14 %)	81	31	$50 \times 10^3$	587	$p$ & $T$ , full scale
Cosham <i>et al.</i> [299]	CO <sub>2</sub>	153.4	5.0	144	146	Wave prop.
Cosham <i>et al.</i> [299]	91.03 % CO <sub>2</sub> , 1.15 % H <sub>2</sub> , 4.00 % N <sub>2</sub> , 1.87 % O <sub>2</sub> , 1.95 % CH <sub>4</sub>	150.5	10.0	144	146	Wave prop.
Drescher <i>et al.</i> [300]	89.8 % CO <sub>2</sub> , 10.1 % N <sub>2</sub>	119.9	19.5	141.9	10	$p$ & $T$
Drescher <i>et al.</i> [300]	80.0 % CO <sub>2</sub> , 20.0 % N <sub>2</sub>	120.8	19.7	141.9	10	$p$ & $T$
Drescher <i>et al.</i> [300]	70.0 % CO <sub>2</sub> , 30.0 % N <sub>2</sub>	120.0	17.3	141.9	10	$p$ & $T$
Jie <i>et al.</i> [301]	CO <sub>2</sub>	39.1	5.0	144	146	Wave prop., gas

two of them, one with pure CO<sub>2</sub> and one with a multicomponent mixture, were discussed in some more detail, including pressure-time traces. The study was motivated by the fact that an understanding of the decompression behaviour is required in order to predict the steel toughness required to arrest a running-ductile fracture. The authors concluded that dense-phase CO<sub>2</sub> has three opposite trends with respect to gas-phase CO<sub>2</sub>: Increasing the initial temperature will increase the required arrest toughness (although this is not always the case for CO<sub>2</sub> mixtures, as discussed by Elshahomi *et al.* [286]); Decreasing the initial pressure will increase the required arrest toughness; The addition of components such as hydrogen, oxygen, nitrogen or methane will increase the required arrest toughness. In the decompression experiments, the measured pressure plateaux were consistently lower than predicted using the GERG-2008 EOS. Further, the measured pressure plateaux increased along the pipe. Cosham *et al.* hypothesized that this may be due to ‘delayed nucleation’, i.e., thermodynamic non-equilibrium, and suggested that the subject requires further investigation in order to understand it in more detail. The effect of impurities (here N<sub>2</sub>) on the saturation pressure, and hence the required arrest toughness, is illustrated in Figure 4a, whereas the influence of initial temperature is illustrated in Figure 4b.

Data from Cosham *et al.* [299] were considered by Jie *et al.* [301], who employed a semi-implicit numerical method to solve the HEM (see Xu *et al.* [309] for more details) with the Peng–Robinson–Stryjek–Vera EOS [310]. It was found that the plateau pressures were overpredicted, particularly for depressurizations starting in the gaseous region. Jie *et al.* [301] hypothesized that this may be due to non-equilibrium effects not being captured by the HEM.

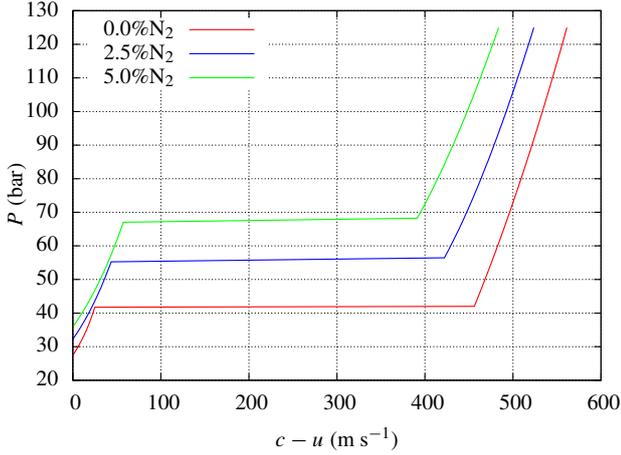
As part of their validation of a homogeneous relaxation model (HRM), Brown *et al.* [297] presented pressure-time traces from two depressurization experiments for pure CO<sub>2</sub>. In the HRM, the phase transition is not instantaneous, as in the HEM. Instead, it is modelled using a ‘relaxation time’. This gave a slightly lower predicted pressure. The presented pressure plots indicated, in our interpretation, that the relaxation versus full-equilibrium modelling was not the main cause of uncertainty with respect to the experimental data. Since the pressure data

were presented on a longer time scale than what is needed to capture pressure waves (10 s), effects of friction and heat transfer to the surroundings could also be relevant.

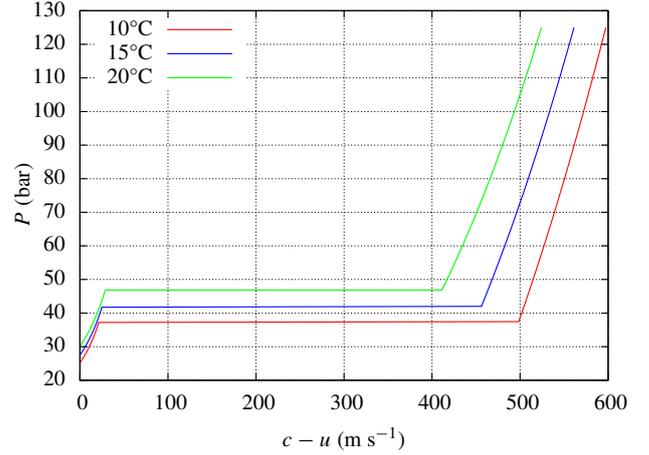
Brown *et al.* [283] presented pressure and temperature measured at different locations during the first part of the depressurization of a 233 mm inner-diameter pipe. Calculations were performed with a HEM and a two-fluid model (TFM) where the mass-transfer between the phases was modelled based on relaxation of enthalpy. Overall, the TFM gave slightly better results than the HEM, but with an increased advantage for the TFM further away from the outlet. The authors found that during the first 1 s of the depressurization, a relatively short relaxation time of  $5 \times 10^{-6}$  s produced good agreement between computation and experiment. After that, however, a longer relaxation time of  $5 \times 10^{-4}$  s gave better agreement. The physical reason why the flow would need shorter time to reach equilibrium during the first part of the depressurization, seems, however, to remain elusive. Both studies [283, 297] employed the Peng–Robinson EOS.

Drescher *et al.* [300] performed depressurization experiments with three binary CO<sub>2</sub>-N<sub>2</sub> mixtures in a tube of length 141.9 m and diameter 10 mm. Pressure and temperature traces were plotted at four different positions, at a time scale including the dry-out point. The cases were modelled using a HEM employing the Friedel [311] friction correlation and a radial heat-transfer model accounting for the heat capacity of the tube. The predicted pressures matched the measured values well, although with a tendency to underprediction. The temperatures were underpredicted to a larger degree. Nevertheless, the calculated dry-out times agreed well with the experiments. In general, computations and experiments matched best near the middle of the tube. The calculated single-phase pressure-propagation velocity was overpredicted when compared to the experiments. This was mainly attributed to the use of the EOS of Peng and Robinson [245].

Munkejord and Hammer [39] expanded the modelling work of Drescher *et al.* [300], adding a two-fluid model (TFM) in which the friction was calculated using the model of Spedding and Hand [312]. Data from Botros *et al.* [296] and Cosham *et al.* [299] were also included in the study. Despite its increased



(a) Decompression speed for pure CO<sub>2</sub> and two CO<sub>2</sub>-N<sub>2</sub> mixtures. Initial pressure 12.5 MPa and initial temperature 15 °C.



(b) Decompression speed for pure CO<sub>2</sub>, at an initial pressure of 12.5 MPa and at three different initial temperatures.

Figure 4: CO<sub>2</sub> decompression-speed dependency of N<sub>2</sub> impurity and initial temperature. The EOS-CG [250, 251] reference EOS is used.

complexity, the TFM could not be said to yield better results than the HEM in general. The authors hypothesized that TFM predictions may be improved with more detailed modelling and experimental studies. The effect of heat-transfer modelling was also studied. For the experiments of Drescher *et al.* [300], the effect of the tube heat capacity was shown to be very large. Not including it yielded far too low temperatures and pressures. Further, for the cases studied, the in-tube heat-transfer correlation of Gungor and Winterton [313] yielded somewhat better results than that of Colburn (see e.g. Bejan [314, Chap. 6]).

The data of Botros *et al.* [296] and Cosham *et al.* [299] were also studied by Elshahomi *et al.* [286], who implemented a 2D HEM employing the GERG-2008 EOS [68]. It seems that for these cases, the main cause of differences between the model of Elshahomi *et al.* [286] and that of Munkejord and Hammer [39], is the different EOS, not the effect of 1D versus 2D.

A technical report by Armstrong and Allason [295], and accompanying documents and data files, have recently been made publicly available. A series of pipe-depressurization experiments with pure CO<sub>2</sub> have been conducted, with full-bore opening and varying restrictions at the outlet. Data were recorded both inside and outside the pipe. We have made an initial study of one of the reported cases, see Section 4.2.

#### 4.2. Depressurization case

To illustrate the modelling of CO<sub>2</sub>-pipeline depressurization, we consider experimental data of Test 4 recently published in a technical report by Armstrong and Allason [295] with accompanying data files. See also Table 9. A pipe of length 200 m, inner diameter 51.92 mm and thickness 4.23 mm is filled with pure CO<sub>2</sub> at a pressure of 101.51 bar and a temperature of 4.9 °C. At time  $t = 0$  s, a rupture disc is cut by an explosive, and the pipe is opened to the atmosphere, such that a decompression wave travels into the pipe.

To calculate the radial heat transfer, we assume that the pipe is made of stainless steel with a density of 8000 kg m<sup>-3</sup>, a

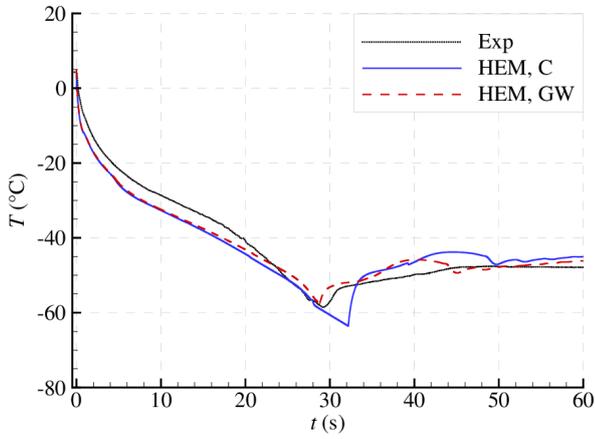
specific heat capacity of 485 J kg<sup>-1</sup> K<sup>-1</sup> and a thermal conductivity of 14 W m<sup>-1</sup> K<sup>-1</sup>. We also assume that the surrounding air temperature is equal to the initial temperature.

The case has been calculated using the homogeneous equilibrium model (HEM) described by Munkejord and Hammer [39] employing the Span-Wagner EOS solved by the method of Hammer *et al.* [244]. For the wall-friction, the correlation of Friedel [311] was employed. A spatial grid of 1200 cells and a CFL number of 0.85 were used. Temperature and pressure are plotted as a function of time at position 5 m (close to the outlet) in Figure 5 and at position 195 m (near the closed end) in Figure 6. The sensitivity to the choice of model for the in-tube heat-transfer coefficient is indicated. The legend ‘C’ denotes the simple correlation of Colburn (see e.g. Bejan [314, Chap. 6]), while ‘GW’ denotes the correlation of Gungor and Winterton [313] accounting for saturated flow boiling.

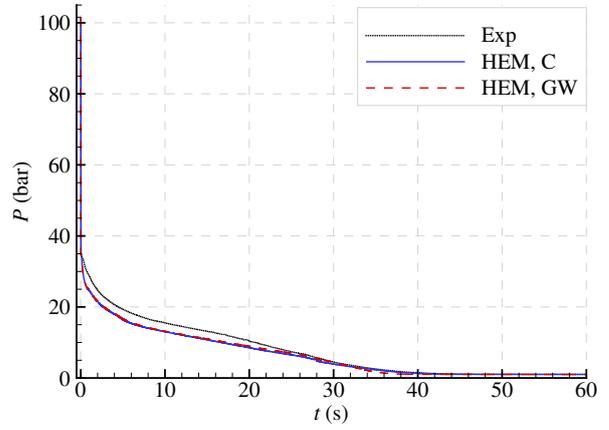
In Figures 5b and 6b, it can be observed that there is good agreement for the pressure, although with a tendency towards underprediction, particularly near the outlet in the first part of the depressurization (Fig. 5b). This is consistent with the results reported by Munkejord and Hammer [39], but in contrast to those of Brown *et al.* [283], where their HEM overpredicted the measured pressure.

For the temperature near the outlet, plotted in Figure 5a, there is also good agreement between computation and experiment. The HEM, both when the Colburn and when the Gungor–Winterton heat-transfer correlation is used, predicts the appearance of solid CO<sub>2</sub> at about 28 s. When all the solid is sublimated, the temperature starts rising. With Gungor–Winterton, this point is predicted at 29 s, which appears to be in very good agreement with the experiment. With Colburn, on the other hand, the predicted minimum temperature appears nearly 3 s late.

The temperature near the closed end of the pipe is plotted in Figure 6a. In the first part of the depressurization, there is good agreement between computation and experiment. After about 30 s, however, the use of the Gungor–Winterton correlation first leads to an underpredicted temperature, and then to a significant

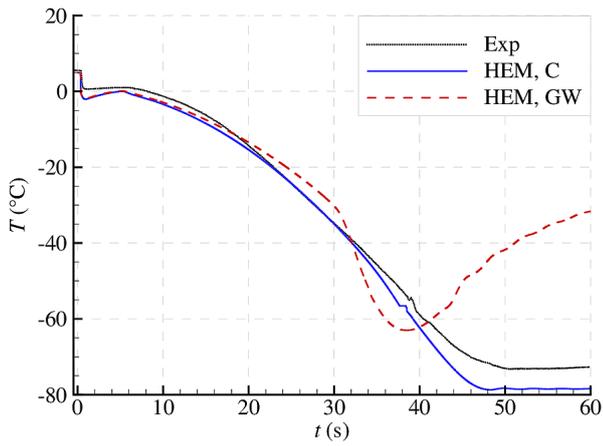


(a) Temperature.

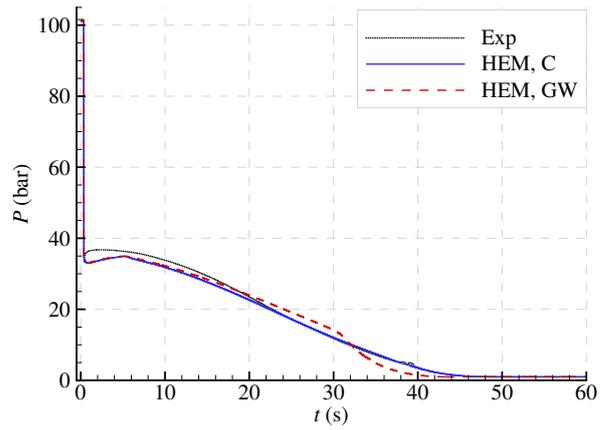


(b) Pressure.

Figure 5: Depressurization case: Comparison of data from experiments (Exp) and homogeneous equilibrium model (HEM) at position 5 m (from the outlet) using Colburn (C) and Gungor–Winterton (GW) heat-transfer coefficient.



(a) Temperature.



(b) Pressure.

Figure 6: Depressurization case: Comparison of data from experiments (Exp) and homogeneous equilibrium model (HEM) at position 195 m (from the outlet, i.e., near the closed end) close using Colburn (C) and Gungor–Winterton (GW) heat-transfer coefficient.

overprediction. The Colburn correlation gives far better results here: At about 38 s, there is a kink in the calculated temperature due to the triple point. It is interesting to note that there is a corresponding feature in the measured temperature at about the same time. After this, both the calculated and measured temperature flatten out, but the calculated temperature is about 5 K lower than measured. The main reason for the difference between the temperature calculated with Gungor–Winterton and with Colburn, is that with the former, the heat transfer is higher, such that the triple point is avoided and no solid is formed. The measured temperature, on the other hand, gives a clear indication that there is solid CO<sub>2</sub> present in the experiment, since the presence of solid CO<sub>2</sub> keeps the temperature down. Flow models should, therefore, be able to take solid CO<sub>2</sub> into account.

Although there are no flow-regime observations for this case, our interpretation of these results is that close to the outlet, there is a strongly dispersed flow regime, where the no-slip assumption in the HEM is not too far off. Near the closed end of the pipe, however, we expect the flow to have a tendency to stratification, for which the HEM cannot account. In view of this, the results presented in Figure 6 for the Colburn correlation are rather better than what we had expected.

Armstrong and Allason [295] presented more data than what we have analysed here, e.g., depressurizations with orifices and pressure and temperature data taken at different positions. A modelling study considering more of the data set would constitute an interesting continuation of this work.

It should also be mentioned that we have accounted for the heat capacity of the pipe, as described by Munkejord and Hammer [39]. The assumption of adiabatic flow would lead to a significant underprediction of temperatures and pressures, although not as dramatic as for the 10 mm tube considered in Case 3 of Munkejord and Hammer [39]. This illustrates the different challenges in pipe-depressurization modelling: The prediction of quantities both near the outlet and near the closed end, as well as capturing both the initial waves, and the slower phenomena involving heat and mass transport.

As alluded to by e.g. Cosham *et al.* [299], detailed experimental observations of the first instants of pipe depressurizations often seem not to be compatible with an assumption of full thermodynamic equilibrium, with measured pressure plateaux lower than predicted. It appears that flow models accounting for ‘delayed nucleation’ may be needed to describe this behaviour. This is of importance e.g. for the modelling of running-ductile fracture in CO<sub>2</sub> pipelines, and it constitutes an interesting avenue for further research.

### 4.3. Running-ductile fracture in CO<sub>2</sub> pipes

For pipelines transporting pressurized fluids, including CO<sub>2</sub>, it is important to ensure that a leak do not form a running ductile fracture, and that any running fracture be quickly arrested [315]. For CO<sub>2</sub> pipelines, ensuring running-ductile fracture arrest will often be a restrictive design criterion. It has been found that a pipeline carrying CO<sub>2</sub> in a dense phase will have higher propensity to running-ductile fracture than a pipeline transporting e.g. natural gas [19, 20, 316]. In simple terms, this

is due to the high saturation pressure reached from a ‘typical’ dense-phase state, as well as the very large difference between the single-phase and two-phase decompression speed illustrated in Figure 4. The fracture propagation is governed by a ‘race’ between the decompression speed in the fluid and the fracture velocity in the steel. If the fracture velocity is faster, the pressure at the crack tip will remain high, and the fracture will propagate. On the other hand, if the decompression speed is faster, then the pressure at the crack tip will fall, and the crack will arrest.

The most common engineering design method against running-ductile fracture, the semi-empirical Battelle two-curve method [317], cannot be directly applied to dense-phase CO<sub>2</sub> pipelines [318]. CO<sub>2</sub> pipelines are commonly equipped with fracture arresters at regular intervals [2, Sec. 4.2.3]. Botros *et al.* [296] recommended at least one to two full-scale burst tests for each design case. Whence there is a need better to understand running-ductile fracture, which is a coupled fluid-structure problem [319].

One hypothesis is that additional insight may be gained by building models representing more of the fluid and structure physics, see Aursand *et al.* [4], Nordhagen *et al.* [320] and the references therein.

Some work has been undertaken in the development of fluid-structure interaction models, in which both the fluid and the steel structure are simulated to predict running-ductile fracture [321–324]. However, there is a need to develop models accounting for the behaviour of CO<sub>2</sub>. Aihara and Misawa [316] presented a model in which the pipe radial displacement was determined by a single parameter, and they showed that a fracture in a pipeline with CO<sub>2</sub> and small amounts of impurities will tend to propagate longer than in natural-gas pipelines. Mahgereteh *et al.* [19] coupled a homogeneous equilibrium model with the fracture-propagation model of Makino *et al.* [325]. Validation cases were presented for natural gas. For a case with CO<sub>2</sub>, they found that the fracture-propagating distance increases for increasing pipeline temperature. Further, they found that larger amounts of impurities in the CO<sub>2</sub> increase the fracture-propagation distance.

A coupled fluid-structure methodology to predict fracture arrest for natural gas and hydrogen was discussed by Nordhagen *et al.* [320], Berstad *et al.* [326]. The pipe was modelled in a finite-element framework using shell elements while the fluid was modelled using a one-dimensional finite-volume method. Good agreement with the burst tests of Aihara *et al.* [327] was obtained. In Aursand *et al.* [20], the model was extended to account for CO<sub>2</sub> properties, using a homogeneous equilibrium model. Coupled-model predictions were compared to uncoupled two-curve models by Aursand *et al.* [284]. The coupled fluid-structure model predicted significantly thicker pipe walls to be necessary for fracture arrest than the uncoupled two-curve models, indicating that the latter may not be conservative for CO<sub>2</sub>. Experimental validation against medium-scale crack-arrest experiments for CO<sub>2</sub> was performed by Aursand *et al.* [328]. The coupled-model calculations showed that the pressure load on a bursting pipeline filled with CO<sub>2</sub> is significantly more severe than in the case of natural gas. This may be one reason why two-curve methods have been found to fail for CO<sub>2</sub>.

For coupled fluid-structure models, the leakage rate will

affect the pressure distribution and hence the forces on the pipe walls. As noted by Aursand *et al.* [4], different flow-modelling assumptions will, in turn, affect the leakage rate. The homogeneous-equilibrium assumption will typically yield the lowest leakage rate, and will therefore be conservative in this context. Expressions to be applied at the outflow boundary for a HEM are given e.g. by Munkejord and Hammer [39], Hammer *et al.* [244]. It is foreseeable that similar expressions may be difficult to derive for more complex flow models. It may then instead be worthwhile to apply the same CFD method as the one employed inside the pipe [329].

More work is needed to validate the above-mentioned coupled models against experiments conducted with CO<sub>2</sub>. As far as we know, the only published results from full-scale pipeline burst tests with CO<sub>2</sub>-rich mixtures are those of Jones *et al.* [318], Cosham *et al.* [330]. In addition, some medium-scale ('West Jefferson') tests have been performed [318, 331]. The scale here relates to the pipeline length; over 100 m for full scale, and around 10 m for medium scale.

Many CO<sub>2</sub>-storage sites are expected to be located offshore. It is therefore relevant to consider the integrity of offshore pipelines. Long running fractures may be a smaller challenge offshore, due to the high surrounding pressure. However, should a pipe rupture occur, it is of interest to estimate the leakage rate and the extent of the plume. Herein, it may be necessary to consider the relatively complex phase behaviour of CO<sub>2</sub>-water mixtures [160]. Some modelling considerations for subsea pipelines were made by Meleddu *et al.* [332]. The leakage of air through a fracture in a pipeline submerged in shallow water was calculated using a 3D CFD model. Herein, the pipe cross-section was approximated to be of a square shape, and the fracture development was prescribed. The modelling results could be compared to available experimental data, and good agreement was obtained for the pressure development. Further, the model was employed to simulate the full-bore rupture of a deep-water CO<sub>2</sub>-transport pipeline, assuming CO<sub>2</sub> and water to be immiscible. An experimental validation of these results would be interesting, but challenging.

#### 4.4. Wave-propagation, equilibrium and flow modelling

Pressure-wave propagation is a determining factor in several phenomena of practical interest. During a pipeline depressurization, the flow will often be choked at the outlet, which means that the local flow velocity is equal to the local pressure-propagation velocity (speed of sound). For typical conditions for CO<sub>2</sub> pipelines, the choking will occur for a two-phase state. As is well known, the single-phase speed of sound is a thermodynamic quantity. For a two-phase state, the case is more complicated, since the observable pressure-propagation speed is a function of the flow topology. The simplest model example is the HEM, where the pressure-propagation speed (or mixture speed of sound) is a function of the gas volume fraction. The two-phase mixture speed of sound is typically lower than both the gas and the liquid speed of sound. The difference between the single-phase and the two-phase speed of sound is one of the factors affecting the propagation of running-ductile fracture in pipelines, see the previous section.

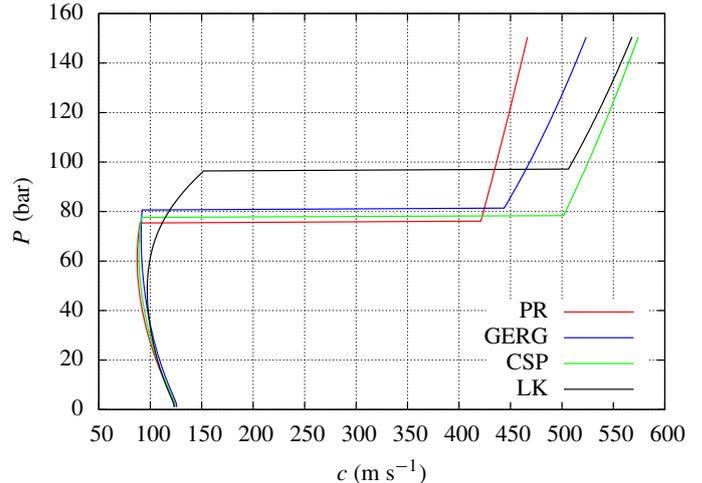


Figure 7: Speed of sound predicted using the Peng-Robinson (PR), GERG-2008 (GERG), a corresponding state approach [260] (CSP) and the Lee-Kesler [259] (LK) equations of state. The CSP method uses Peng-Robinson with van der Waals mixing rules to scale the propane properties calculated using the MBWR32 [247, 261] equation. The CO<sub>2</sub>-H<sub>2</sub>-N<sub>2</sub>-O<sub>2</sub>-CH<sub>4</sub> mixture and initial conditions of Cosham *et al.* [299] are employed, see Table 9.

Judging from the pipe-depressurization data presented by Cosham *et al.* [299], it appears that the flow may be in non-equilibrium, and more so during the first instants of the depressurization and close to the outlet. To our knowledge, it remains to develop and validate flow models properly accounting for this effect. This implies that flow models should not only allow slip between the phases, but that they should also accommodate non-equilibrium in one or more of the quantities temperature, chemical potential and pressure. Therefore, despite the good results in many cases (see Section 4.2), the HEM is not expected to be the ideal pipe-depressurization flow model. This is linked to the fact illustrated in Figure 3b, namely, that in the HEM, the speed of sound is discontinuous at the phase boundary, and moreover, it is zero at the triple point [287, Sec. 2.8.1]. This property is not believed to be physical, and it causes difficulties when developing numerical methods and performing simulations.

To illustrate that different models give very different speed-of-sound predictions, particularly above the saturation pressure, four common EOSs have been used to plot the equilibrium speed of sound for the Cosham *et al.* [299] mixture in Figure 7. Only the GERG-2008 model has been tuned to experimental speed-of-sound data, while the other EOSs mostly have been tuned to equilibrium data.

From a modelling viewpoint, a set of physical assumptions leads to a mathematical flow-model formulation. This formulation has inherent wave-propagation velocities. These velocities may be compared to experimental observations and this may serve as validation tests to be performed for the flow model.

Flow models allowing some degree of non-equilibrium are often formulated as *relaxation models*, see Aursand *et al.* [4]. Munkejord [333, 334] studied pressure relaxation in a two-fluid model. With instantaneous relaxation, the relaxation model approached the single-pressure model, but the numerical relaxation

procedure introduced considerable numerical smearing.

Flåtten *et al.* [335] derived expressions for the wave velocities a multicomponent flow model with thermal relaxation. Martínez Ferrer *et al.* [336] studied temperature and velocity relaxation for the two-phase case. Flåtten and Lund [337], Lund [338] developed a relaxation-model hierarchy for no-slip two-phase flow models. It was shown that that the relaxed model always has a lower speed of sound than the relaxation model. In other words, the lowest two-phase mixture speed of sound is inherent in the HEM. The relaxation-model hierarchy was expanded by Linga [339], allowing slip between the phases.

Saurel *et al.* [340] considered a no-slip two-phase flow model with temperature and chemical-potential relaxation, albeit infinitely fast, near the gas-liquid interface. Zein *et al.* [341] studied a similar model, but with balance equations for the individual phasic velocities. A validation test was performed against data from a dodecane liquid-vapour shock tube. Rodio and Abgrall [342] presented an approach based on the discrete-equations method aimed at modelling flexibility and computational efficiency. So far, these models [340–342] employed the stiffened-gas EOS [343, 344]. We are not aware that these models have been validated for CO<sub>2</sub>. A HEM using the stiffened-gas EOS for each phase was explored by Lund *et al.* [345], but lacked experimental data to compare with.

Most relaxation models so far have assumed the phase transfer either to be ‘fast’, or to be governed by a prescribed relaxation time. Future models should incorporate physical modelling of the phase transfer accounting for the relevant kinetics. As shown in the initial study by Lund and Aursand [346], statistical rate theory may provide a framework to do so.

Benintendi [347] discussed the effect of non-equilibrium phase transitions for expansions of liquid and supercritical CO<sub>2</sub>, focusing on jet-flow characteristics after the stagnation point. Deficiencies of the HEM were described, and the author hypothesized that using a relaxation model (HRM) may improve the prediction of observed CO<sub>2</sub> expansion properties. One simplified steady-state numerical calculation was made along an expansion path, but the model is not directly applicable for handling non-equilibrium phase transitions in a CFD code.

Accounting for delayed homogeneous nucleation appears to be necessary to obtain a correct prediction of pressure and temperature for fast depressurizations. Further, the triple-point singularity resulting from the full equilibrium assumption must be overcome using non-equilibrium thermodynamics.

Tian *et al.* [348] performed a theoretical analysis of the liquid-to-vapour expansion mechanism in CO<sub>2</sub>. They considered the critical energy barrier of a bubble nucleus as a function of saturation temperature. Using non-equilibrium thermodynamics, they calculated the entropy production during CO<sub>2</sub> expansion. Zero energy penalty was found at the critical point where the phases are identical. For lower pressures, further down the saturation line, the energy penalty (entropy production) increases.

Heermann *et al.* [349] performed molecular-dynamics simulations to determine the spinodal for pure CO<sub>2</sub>. Fast temperature quenching and droplet nucleation relevant for polymer foams produced with a CO<sub>2</sub> blowing agent were of interest. Therefore, only the gas spinodal was studied. The same atomistic

approach was used to calculate the saturation properties of CO<sub>2</sub>. The results were in qualitatively good agreement with the predictions of the Span-Wagner EOS. However, the liquid density predicted by the molecular-dynamics simulations became too low for increasing temperature. The meta-stable region mapped from the molecular simulation was much smaller than the meta-stable region predicted from the van der Waals EOS and a virial expansion EOS.

#### 4.5. Closure relations for CO<sub>2</sub>

Existing flow maps and correlations for oil, natural gas and water in transport pipelines cannot necessarily be expected to be accurate for CO<sub>2</sub>-rich mixtures, due to the significantly different thermodynamic and transport properties. Most of the flow maps and pressure-drop measurements and correlations for CO<sub>2</sub> are taken for tubes and channels in the millimetre range, often with heat-exchanger applications in mind, see e.g. [350–353].

Aakenes *et al.* [354] considered experimental data for frictional pressure drop in a 10 mm inner-diameter tube. See also de Koeijer *et al.* [37]. The data were compared to the model of Friedel [311] and that of Cheng *et al.* [353]. Although the latter was developed specifically for CO<sub>2</sub>, the former fitted the data better, with a standard deviation of 9.7%. This is perhaps because of its larger experimental database.

Cho *et al.* [305] performed an experimental study of the two-phase pressure drop for the flow of a CO<sub>2</sub>-N<sub>2</sub> mixture in a tube of inner diameter 3.86 mm, using the same facility as in the study of Huh *et al.* [304]. The results were compared to different pressure-drop correlations, and rather large mean absolute errors in excess of 300% were observed. It remains to provide an explanation for the deviations.

## 5. Ship transport of CO<sub>2</sub>

CO<sub>2</sub> transport with ship is interesting in scenarios involving CO<sub>2</sub> sources close to the coast and offshore storage. Since ships are more flexible than pipelines, ship transport may be preferable for early CCS deployment, where the CO<sub>2</sub> quantities are small.

### 5.1. Techno-economic considerations

Publicly available work on ship transport of liquid CO<sub>2</sub> started appearing the early 2000s with several patents of Mitsubishi Heavy Industries [355]. Kaarstad and Hustad [356] conducted an overall assessment of ship and pipeline transportation of CO<sub>2</sub> to an oil field in the North Sea. The first detailed technical and economic study on CO<sub>2</sub> ship transport, by Aspelund *et al.* [357], recognized the potential role for shipping in developing the use of CO<sub>2</sub> for EOR, identifying the financial incentive of EOR, giving a value to CO<sub>2</sub>. Further benefits of ship transport pointed out by this study were the flexible collection of CO<sub>2</sub> from several low-costs sources, flexibility for delivery to different locations and the relatively low capital expenditure for ship-based transport compared to pipeline transport.

When comparing ship transport to pipeline transport it is intuitive that transport distance is a key parameter. Economic studies show that long transport distance favours ship transport

of CO<sub>2</sub> over pipe transport [358]. Technical-economic studies on ship transport of CO<sub>2</sub> were performed by Roussanaly *et al.* [359] who compared costs for CO<sub>2</sub> transport by ship or by onshore pipeline between Le Havre and a hub at Rotterdam, with the concept of onward transport for storage or EOR from there. In this specific case it was concluded that shipping cost around 10 % more. Skagestad *et al.* [360] pointed out that the liquefaction and operational costs are the main cost drivers for the ship, and capital investment cost is the main driver for pipeline transport.

Aspelund *et al.* [357] assumed pure CO<sub>2</sub> transported in a state close to the triple point, e.g. 6.5 bar and the corresponding saturation temperature, approximately  $-52\text{ }^{\circ}\text{C}$ . These conditions are used in most later studies on CO<sub>2</sub> ship transport. However, a study by Nam *et al.* [361] optimized conditions over an entire transport chain, including pipeline sections and intermediate storage, and concluded on global optimum conditions of 10 bar and  $-39\text{ }^{\circ}\text{C}$ .

Vermeulen [358] published a knowledge-sharing report considering the entire chain of liquid CO<sub>2</sub> transport by ship. Several types of infrastructure for offshore offloading system were considered, and well simulations were performed to characterize the temperature dynamics stemming from the batchwise injection of CO<sub>2</sub>. The hydrate temperature in the reservoir was identified as a defining criterion for the injection, requiring heat exchangers for conditioning at the injection site. The shipping solution considered was a modified liquefied petroleum gas (LPG) carrier with a cargo capacity of 30 000 m<sup>3</sup>. The report encompassed most aspects of CO<sub>2</sub> transport by ship, but did not address impurities of CO<sub>2</sub>, determined by the specification of the captured CO<sub>2</sub> and the liquefaction process.

Omata [362] considered LPG carriers and transport of saturated liquid at  $-10\text{ }^{\circ}\text{C}$  (2.65 MPa to 2.8 MPa). The report covers the technical and economic feasibility of a concept for CO<sub>2</sub> transport using a carrier ship with injection equipment on board, to deliver directly to a subsea injection wellhead. It argues that in regions, such as Eastern Asia, where bulk resources are frequently traded long distances internationally by sea, it makes sense to consider the same for CO<sub>2</sub> transport.

Brownsort [363] summarized literature regarding CO<sub>2</sub> ship transport with the main purpose of EOR. It was pointed out that many publications do not debate liquefaction process options, focusing instead on a single process, which may be selected from corporate experience, but without clear justification.

The general conclusion from the CO<sub>2</sub> ship-transport studies are that this is technically feasible, albeit at a generally higher unit price than transport by pipeline. As mentioned earlier, this depends on the transport distance. Longer transport distance favours ship transport. However, there are still open technical questions, e.g., regarding the liquefaction process, the injection system and the well integrity as well as unloading time.

## 5.2. Vessel depressurization

The study of vessel depressurizations appears to be relevant for ship-transport of CO<sub>2</sub> and to other parts of the CO<sub>2</sub> chain where vessels are employed. Even though during normal unloading, the pressure in the storage vessels will be maintained by gas

injection, accidental and uncontrolled depressurization might happen. Experimental data from vessel depressurizations could also be useful for model verification. This subject has received limited attention so far.

The blowdown of CO<sub>2</sub> from initially supercritical conditions was studied by Eggers and Green [364], Gebbeken and Eggers [365], motivated by the use of CO<sub>2</sub> in food-processing technology. The data may serve as validation cases for models involving CO<sub>2</sub> with phase transition induced by depressurization and heat transfer. Fredenhagen and Eggers [366] extended the study to CO<sub>2</sub>-N<sub>2</sub> mixtures and presented a model based on local thermodynamic equilibrium and a drift-flux phase slip. The data of Gebbeken and Eggers [365] were considered in the modeling study of Zhang *et al.* [367] aimed at the safety analysis of supercritical water-cooled nuclear reactors.

Han *et al.* [368] studied the temperature and pressure development in 4.75 mm tubes used for the controlled depressurization of a CO<sub>2</sub> vessel.

Vree *et al.* [369] studied the depressurization of pure CO<sub>2</sub> in a tube of inner diameter 50 mm and length 30 m wound up in a coil of diameter 1.94 m and height 1.25 m. We expect the results to lie somewhere between those of vessels and straight tubes. The effect of nozzle sizes between 3 mm to 12 mm was investigated, as was the effect of depressurizing from the lower or upper end of the coil. The coldest temperature was observed for depressurization from the upper end of the coil.

## 5.3. Boiling liquid expanding vapour explosion

Boiling liquid expanding vapour explosion (BLEVE) may occur in storage and transportation of high-pressure liquefied CO<sub>2</sub>. If the containing pipe or vessel ruptures, violent boiling of superheated CO<sub>2</sub> might cause a destructive shock wave. In Worms, Germany, a catastrophic failure of a liquid CO<sub>2</sub> storage vessel resulted in three fatalities, additionally eight people injured and significant material damage to a production facility [370]. A comprehensive review of the BLEVE phenomenon was presented by Abbasi and Abbasi [371].

Bjerketvedt *et al.* [372] conducted small-scale experiments with CO<sub>2</sub> BLEVE. By placing dry ice in a plastic container and applying heat, a phase change and pressure increase was induced. The pressure was increased until the tube ruptured, and pressure waves were measured at different distances from the container. A need to understand the boiling mechanisms of metastable CO<sub>2</sub> was identified. Bjerketvedt *et al.* concluded that there is a need for EOS validation and large-scale experiments to develop and validate CFD codes to perform risk analysis. Later, the same group performed rapid depressurization experiments of liquid CO<sub>2</sub> in a vertical shock tube [373]. With the aid of a high-speed camera, the evaporation wave propagating into the liquid was studied. A near-constant velocity of 20 m s<sup>-1</sup> to 30 m s<sup>-1</sup> of the liquid-vapour front was reported. The initial pressures were 3.5 and 5.5 MPa. Due to missing temperature and pressure measurements, the authors could not conclude regarding the thermodynamic path of the fluid.

van der Voort *et al.* [374] measured blast waves after fracturing 40 l liquid CO<sub>2</sub> bottles. Two cutting charges installed on

opposite sides of the bottles were used in order to induce a fast and complete rupture of the CO<sub>2</sub> bottle. Simulations employing the Euler equations in 1D and 2D using simplified thermodynamics were compared with the measured blast wave, to give a qualitative fit. In order to give more realistic predictions of the BLEVE blast wave, explicit modelling of phase transition and proper fluid property models are required. The measured blast wave was disturbed by the initial detonation of the cutting charges and reflection from the walls of the test bunker.

Building on these experiments, van der Voort *et al.* [375] conducted 12 experiments using 401 liquid CO<sub>2</sub> bottles to test the temperature dependence of the BLEVE problem. The temperature range was from  $-25.4^{\circ}\text{C}$  to  $21.3^{\circ}\text{C}$ . The motivation was to evaluate the risk of BLEVE occurring below what the authors referred to as the homogeneous nucleation temperature. With data from a reference experiment with an empty bottle, some of the measurement disturbance from the initial detonation of the cutting charges could be removed. The conclusion regarding the homogeneous nucleation temperature remains, however, unclear.

#### 5.4. Flow in wells

Whether the CO<sub>2</sub> has been transported by pipeline, ship, or other means, it will have to be injected into a reservoir through a well. Numerical models to perform calculations of transient scenarios in wells will have many similarities with those for pipelines.

For CO<sub>2</sub> injection into depleted gas reservoirs, or into relatively shallow reservoirs, pressures will be relatively low, such that CO<sub>2</sub> phase change will be more likely than what it usually is for EOR [376].

Many of the existing well-flow models for CO<sub>2</sub> are aimed at capturing essentially steady-state solutions, e.g. [377, 378], or slow transients. Cronshaw and Bolling [379] developed a finite-difference model for the flow of single- or two-phase CO<sub>2</sub> in wellbores, accounting for conduction to the surroundings. A semi-implicit integration procedure was employed. The thermophysical properties were taken from look-up tables. The solubility of water in liquid CO<sub>2</sub> and that of CO<sub>2</sub> in liquid water were neglected. The flow transients were assumed to be sufficiently slow, so that kinetic-energy changes across control volumes could also be neglected.

Pan *et al.* [380] developed a transient drift-flux model (DFM) for two-phase CO<sub>2</sub>-brine mixtures to calculate leakages through the wellbore. A DFM was also studied by Lu and Connell [381, 382]. The Peng and Robinson [245] EOS was employed, with the assumption of full thermodynamic equilibrium. The computations included the effect of transient boundary conditions at the well inlet.

Ruan *et al.* [383] employed Fluent® to study the effect of water convection in the annulus surrounding the well assuming 2D axisymmetry. Musivand Arzanfudi and Al-Khoury [384] considered the leakage of CO<sub>2</sub> through an air-filled abandoned wellbore using a mixed finite-element discretization scheme. A main aim was to achieve a high numerical efficiency.

de Koeijer *et al.* [385] identified a need for experiments on shut-ins and depressurization in CO<sub>2</sub> injection wells. In order

to characterize the reservoir, shut-in and depressurization operations are performed on the well. Especially the interaction between CO<sub>2</sub> and brine in the reservoir is of interest. A new infrastructure, drilling a 200 m to 250 m deep well, was suggested.

For safety, and to maintain the purpose of CCS, it is essential to ensure the integrity of CO<sub>2</sub> wells. Thermal cycling is one factor which can lead to debonding at the casing-cement or cement-rock interface. CO<sub>2</sub> injection may impose lower temperatures and stronger temperature variations on wells than what is done for oil and gas production. Therefore, it is of great interest to develop modelling tools which can assess various designs and operational procedures. Lund *et al.* [386] developed a radial heat-transfer model designed to account for the discontinuous thermal properties at the casing-cement and cement-rock interface. Good agreement with laboratory experiments was obtained. Future work should include the assessment of radial asymmetry, and the coupling to well-flow and reservoir models.

## 6. Conclusions

Although CO<sub>2</sub> is transported in various ways today, the amount required for full-scale CCS implementation motivates the search for solutions being as safe and reliable as required and as efficient as possible. To do this, simulation tools handling the transient flow of single- and multiphase CO<sub>2</sub> and CO<sub>2</sub>-rich mixtures inside, and out of, pipes and vessels are needed to perform calculations relevant for design, operation and safety. Today's models are in need of improvement with respect to both fluid flow and thermophysical properties.

The risk associated with CO<sub>2</sub> pipelines has been evaluated to be very low, but the fracture propensity must be successfully mitigated. Today's semi-empirical fracture-propagation models cannot be applied to dense-phase CO<sub>2</sub> pipelines, and it has been recommended to perform at least two full-scale burst tests for each design case. The development of coupled fluid-structure fracture-propagation control models may lead to a better predictive capability.

Two-phase flow conditions can be expected to occur during various transient events even for systems designed to operate in the single-phase state. Such events can be varying CO<sub>2</sub> supply, start-up, shut-in or depressurization. Therefore, there is a need to develop validated simulation tools able to accurately predict these situations. Existing two-phase flow modelling tools can be expected to have moderate accuracy due to the limited data for CO<sub>2</sub> flow.

Depressurization experiments of pipes and tubes constitute one type of input needed for the development of fracture-propagation models, and two-phase flow models in general. It appears that two-phase flow models aiming to accurately describe rapid depressurizations need to take non-equilibrium effects into account. Among the different two-phase flow model formulations available today, there is not a 'generally preferred' one. Nevertheless, the relatively simple homogeneous equilibrium model has yielded good results in several cases. For depressurizations down to atmospheric conditions, models will, in many cases, need to take the formation of dry ice into account.

This was shown in our case study considering expansion-tube experimental data.

Regarding depressurizations of tubes, the shorter the time scale, the better the description provided by pure depressurization fluid dynamics and thermodynamics. For longer times, effects from friction, flow topology and heat transfer enter into play, rendering the interpretation of both experimental and modelling results complex.

The depressurization of vessels have, in many respects, a simpler flow configuration than the depressurization of pipes. Therefore, such data should be useful for validation of thermo-physical and heat-transfer models relevant for CO<sub>2</sub> transport.

Regarding ship-transport of CO<sub>2</sub>, one of the main challenges appears to be the optimal chain design. It has to include the liquefaction, conditioning and possible processing at the injection site. Issues like well integrity and the response of the CO<sub>2</sub> reservoir should also be considered. This will require good knowledge of the relevant CO<sub>2</sub>-rich fluid properties, as well as flow in the well, the interaction of brine and CO<sub>2</sub>, etc. There also seems to be a need for a better understanding of the safety aspects of transporting CO<sub>2</sub> in large vessels, such as the possible occurrence of boiling liquid expanding vapour explosion (BLEVE).

Removing a large portion of impurities produced by CO<sub>2</sub> capture processes could have a high cost. Hence the effect of impurities in CO<sub>2</sub>-rich mixtures, which could be different in CCS than in the current US CO<sub>2</sub>-transportation pipeline systems, must be known for cost and energy optimization. Even if strict purification standards are enforced, the impact of impurities will still have to be predicted in order to design efficient conditioning processes or to understand CO<sub>2</sub> injection processes or EOR or storage reservoir behaviour. For some properties, relatively accurate equilibrium models exist for pure CO<sub>2</sub>. There are also thermodynamic models addressing the impact of impurities, but mixture models for transport properties are less developed.

Fiscal metering will be needed in order to facilitate government control and transactions in a future CCS market and the lack of accurate property models could have large cost impacts.

Currently, the best property models are empirical in nature, and hence cannot be more accurate than the experimental data to which they are fitted. In order to model mixtures, complete binary mixture data sets are desired, with ranges in temperature, pressure, and composition beyond what are expected for the given application. In the current work, the data situation of some important fluid equilibrium properties for CO<sub>2</sub>-rich mixtures has been surveyed, combining and extending a number of more specialized reviews in the literature. Data for phase behaviour, density, speed of sound, viscosity, and thermal conductivity have been investigated, primarily for binary mixtures between CO<sub>2</sub> and 17 other components. With regard to density and vapour-liquid equilibria (VLE), the data situation for binary mixtures between CO<sub>2</sub> and water and the most common components in natural gas, like methane and nitrogen, appears to be satisfactory. For other relevant impurities, like for instance O<sub>2</sub>, there are large holes in the data sets for density and VLE. For other binary systems, like for instance CO<sub>2</sub>-COS and CO<sub>2</sub>-NO, neither VLE nor density data have been found.

In addition to VLE, phase equilibria involving more than one liquid phase (VLLE) and equilibria involving solids / hydrates have been investigated. In general, there are very little experimental data for such phase equilibria, as well as for speed of sound, viscosity, and thermal conductivity. In many cases, there is either no data or only a single data set available per binary mixture system and phase even for the most common impurities, covering at best only a small part of the region of interest in terms of temperature, pressure, or composition. With regard to thermal conductivity, even the most reputable current model for pure CO<sub>2</sub> is still not based on data in the high-temperature zero density region or the important liquid phase.

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